

□ Limits for Compact Stellarators: Are they Real?

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With acknowledgements to M.C. Zarnstorff¹, A. Ware² for major contributions

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ARIES-CS Project Meeting
24 February 2005
General Atomics, San Diego CA

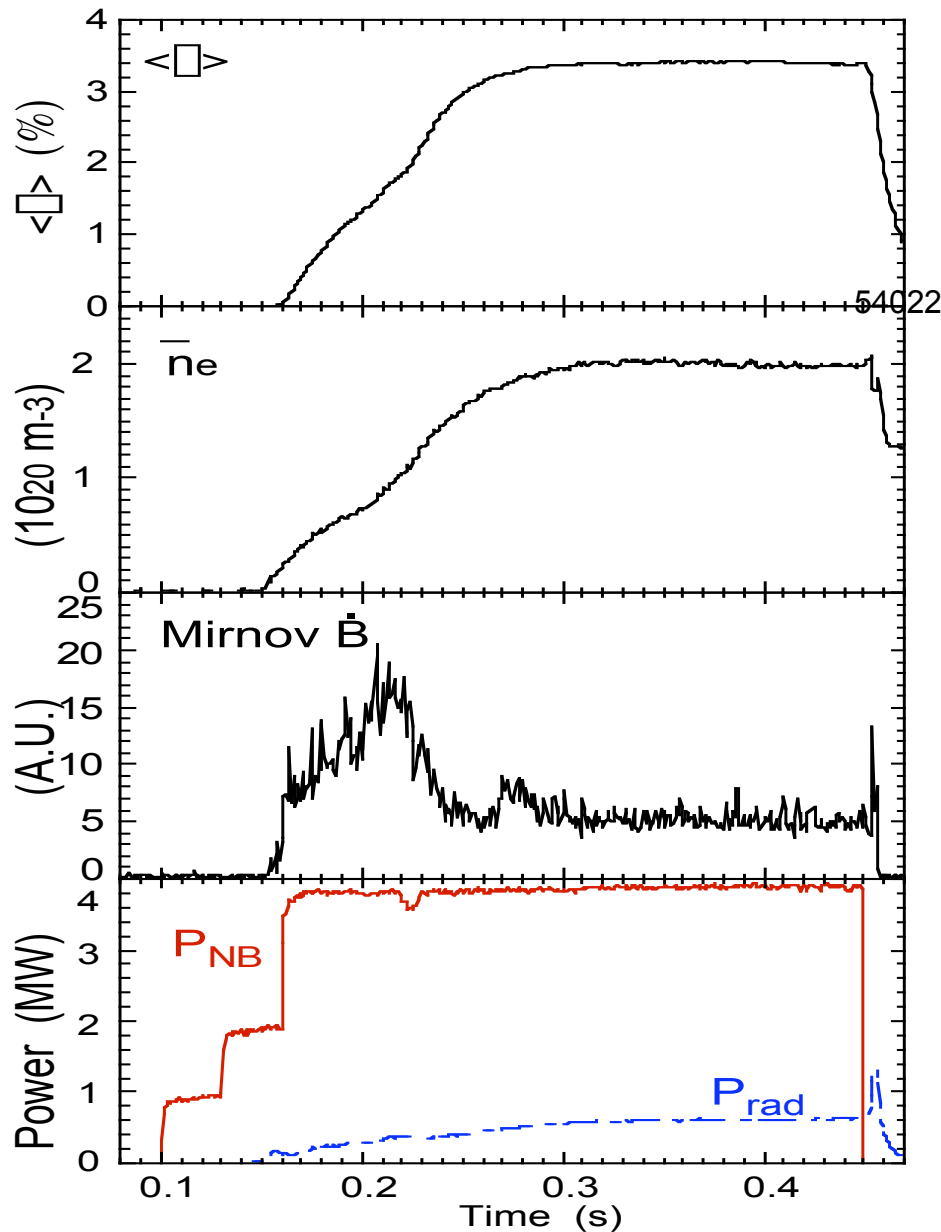
W7-AS and LHD Have Exceeded the Predicted Ideal MHD β Limits

- W7-AS: Achieved $\langle \beta \rangle = 3.4\%$
(M.C. Zarnstorff and A. Weller)
 - High Density Low T_e
 - MHD activity in early medium β phase
 - Robustly achieved for $B = 0.9$ to 1.1 T and varying heating methods
 - Predicted ideal MHD stability limit $\beta \sim 2\%$

LHD Results Are Similar to W7-AS

- LHD: Achieved $\langle \beta \rangle \sim 4\%$
(S. Sakakibara and N. Nakajima)
 - Low Density High T_e
 - 2/1 MHD activity in core for $\beta < 2.5\%$
 - No core MHD observed at high β
 - Edge modes observed for $\beta > 3.4\%$
 - 1/1 surface at $\beta > 0.9$
 - May set β limit
 - Predicted interchange limit at low β is clearly violated
 - Resistive and ideal both unstable

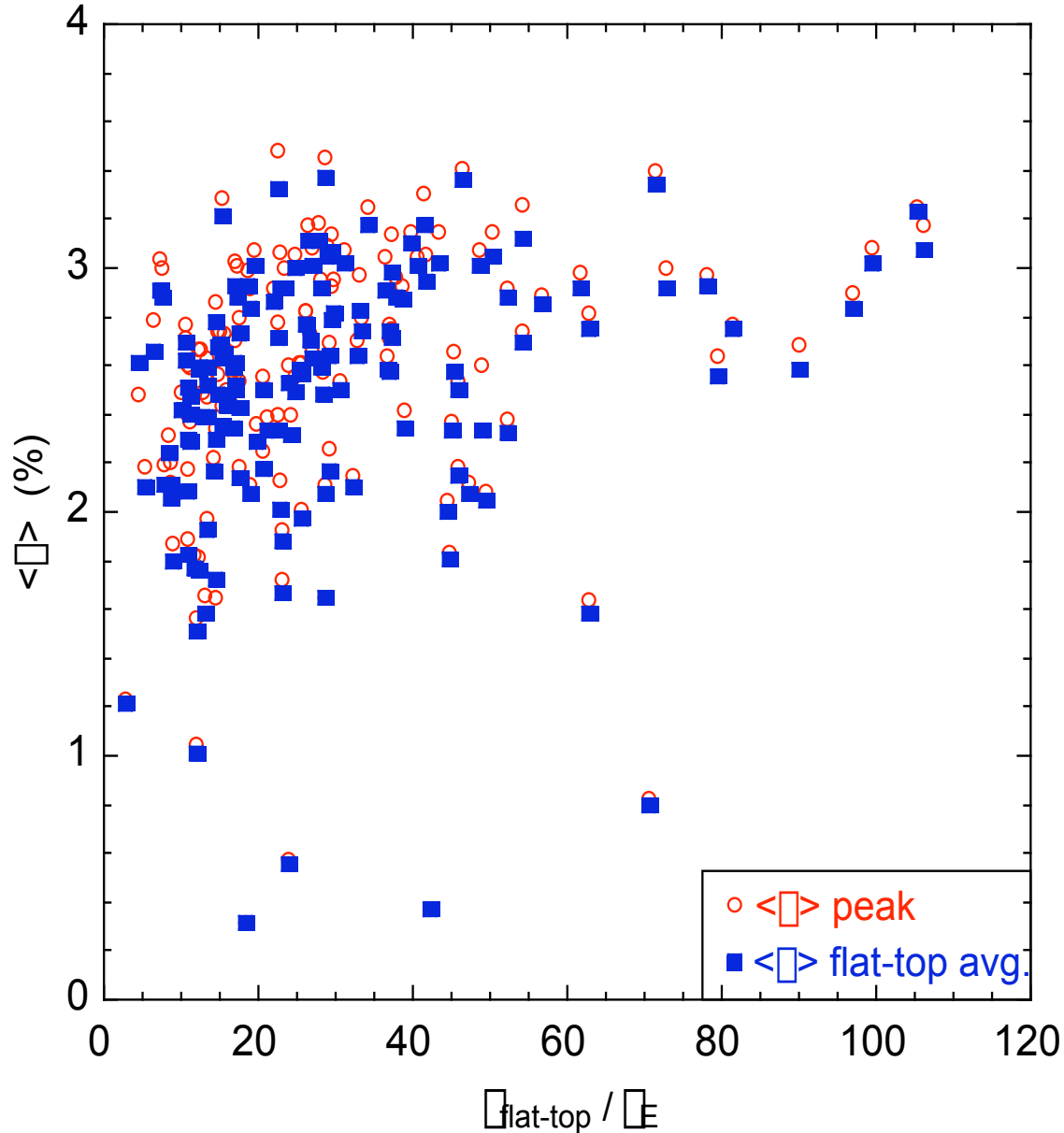
Quiescent Quasi-stationary Discharge: $\beta \approx 3.4\%$



- $B = 0.9$ T, $i_{\text{vac}} \approx 0.5$
- Almost quiescent high- β phase, MHD-activity in early medium- β phase
- β not limited by any detected MHD-activity.
- $I_p = 0$: local currents may exist
- Similar $\beta > 3.4\%$ plasmas achieved with $B = 0.9 - 1.1$ T with either NBI-alone, or combined NBI + OXB ECH heating.
- **Much higher than predicted β limit $\sim 2\%$**

(M.C. Zarnstorff)

$\langle \beta \rangle > 3.2\%$ maintained for $> 100 \tau_E$



- Peak $\langle \beta \rangle = 3.5\%$
- High- β maintained as long as heating is maintained
- $\tau_{\text{flat-top}}$ peak \approx $\tau_{\text{flat-top}}$ flat-top \approx very stationary
- **Duration and β not limited by onset of observable MHD**

What limits the observed β value ?

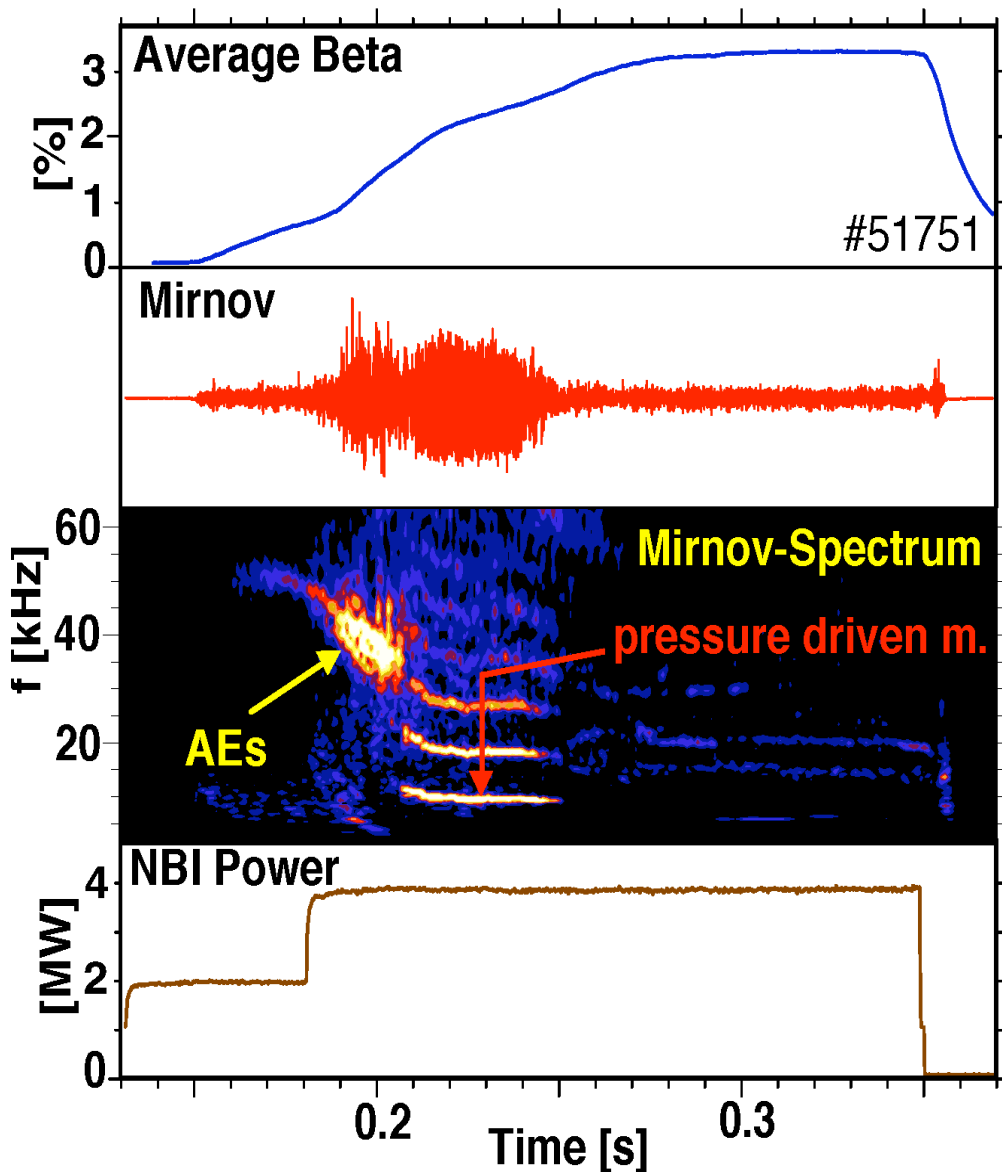
(M.C. Zarnstorff)

MHD Activity is Sometimes Observed in W7-AS at Intermediate β

- $m=2, n=1$ pressure driven modes.
Sometimes also $m=3$ or 5
Does not usually strongly affect confinement
- Alfvénic instabilities at low density
- $(2,1)$ tearing modes with significant $I_p < 0$
(increasing ι) and tokamak-like shear
- High n instabilities at very low T_e

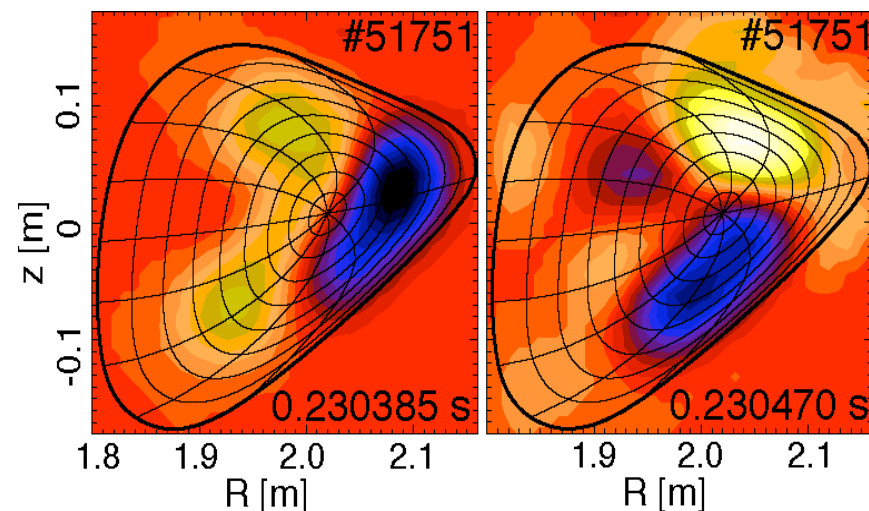
(M.C. Zarnstorff)

Pressure Driven Modes Observed at Intermediate β



- Dominant mode $m/n = 2/1$
- Modes disappear for $\beta > 2.5\%$
(inward shift of iota = 1/2 surface?)

X-Ray Tomograms

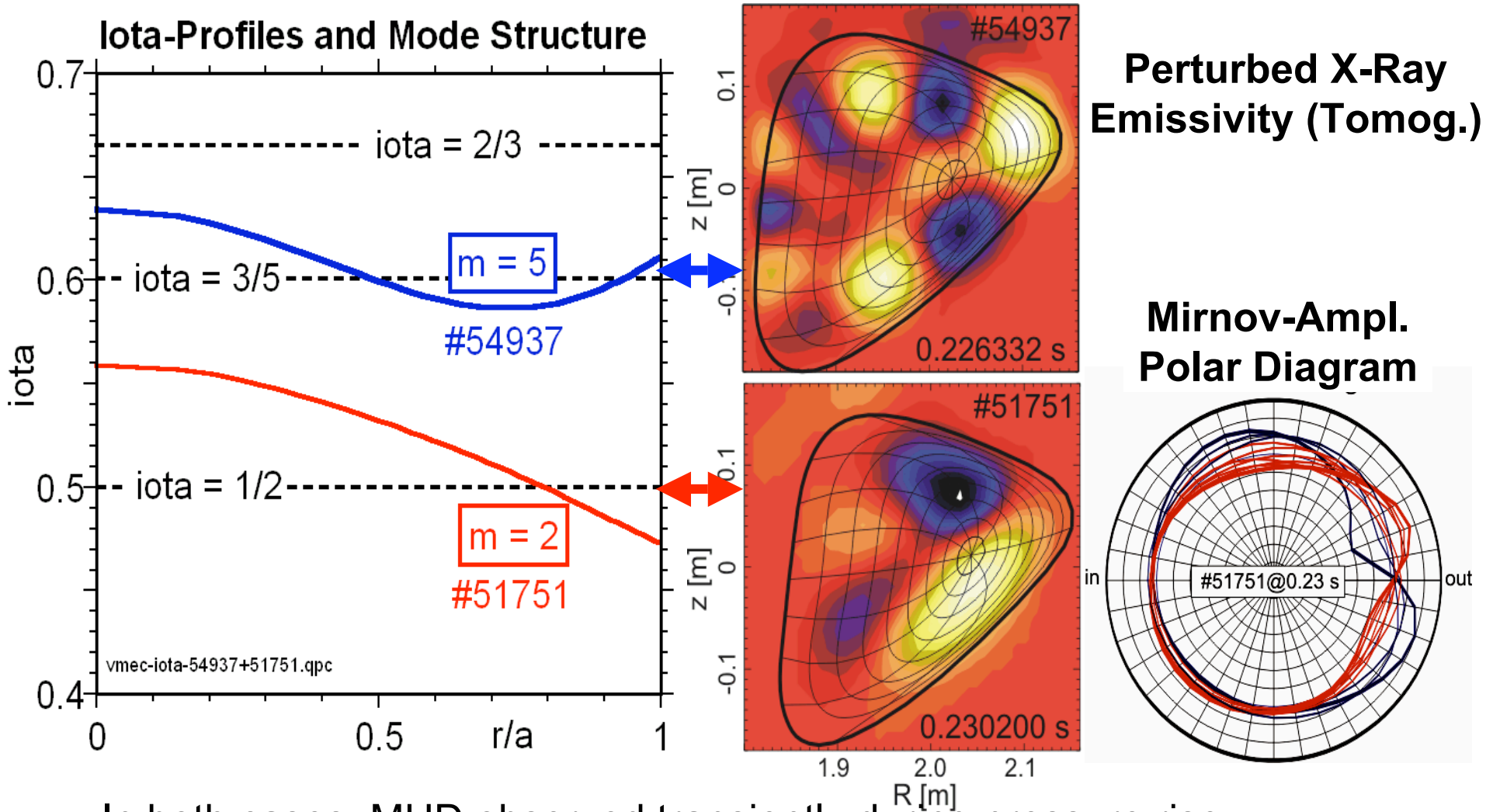


- Reasonable agreement with CAS3D and Terpsichore linear stability calculations: Predicted threshold $\beta < 1\%$

Does not inhibit access to higher β !
Linear stability threshold is not indicative of β limit.

(M.C. Zarnstorff)

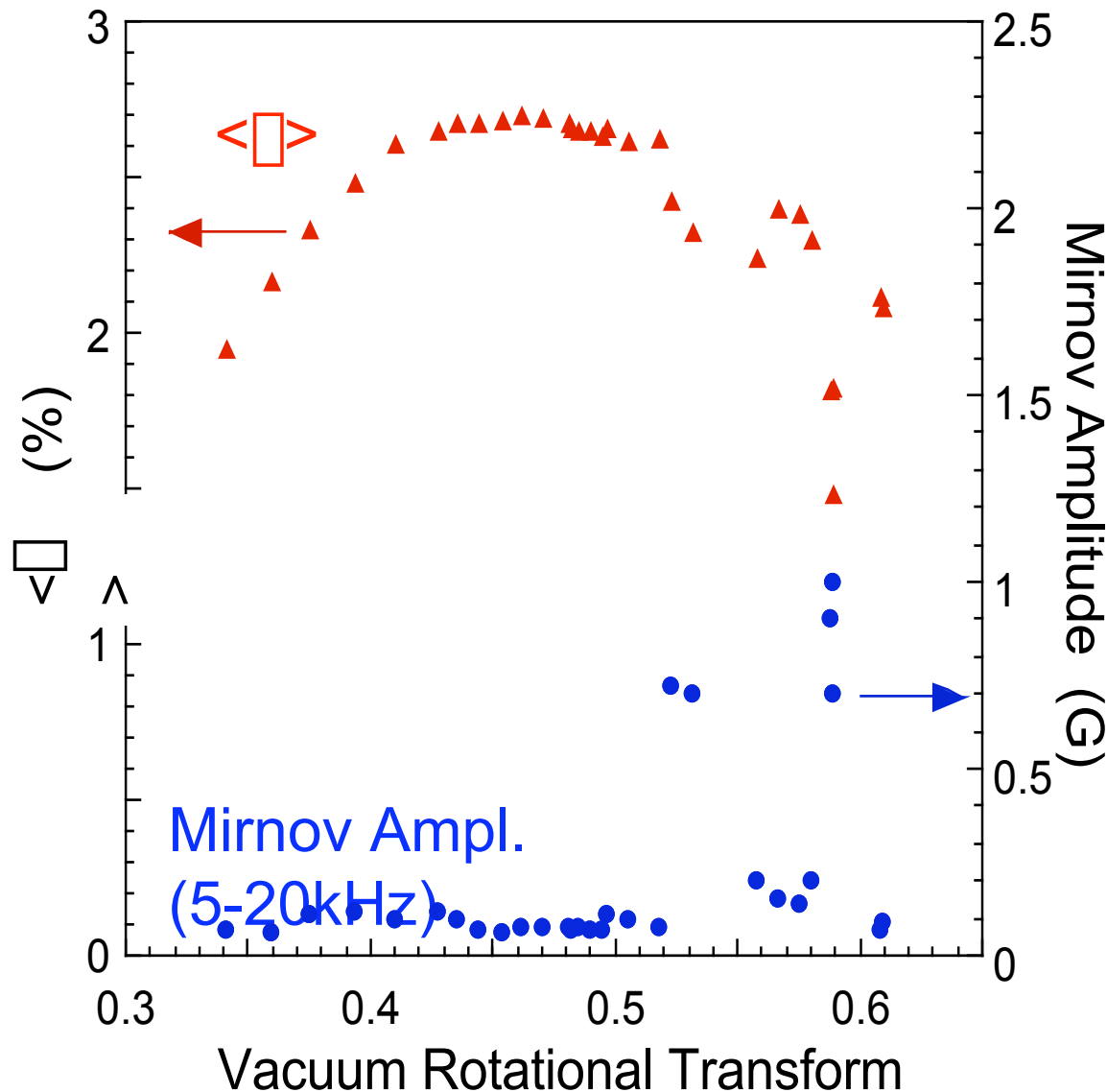
Observed Mode Structure Corresponds to Near-Edge Iota (VMEC)



- In both cases, MHD observed transiently during pressure rise. Edge iota drops as β increases, due to equilibrium deformation.
- Strong ballooning effect at outboard side

(M.C. Zarnstorff)

Low-mode Number MHD Is Very Sensitive to Edge Iota During Flat-top in W7-AS



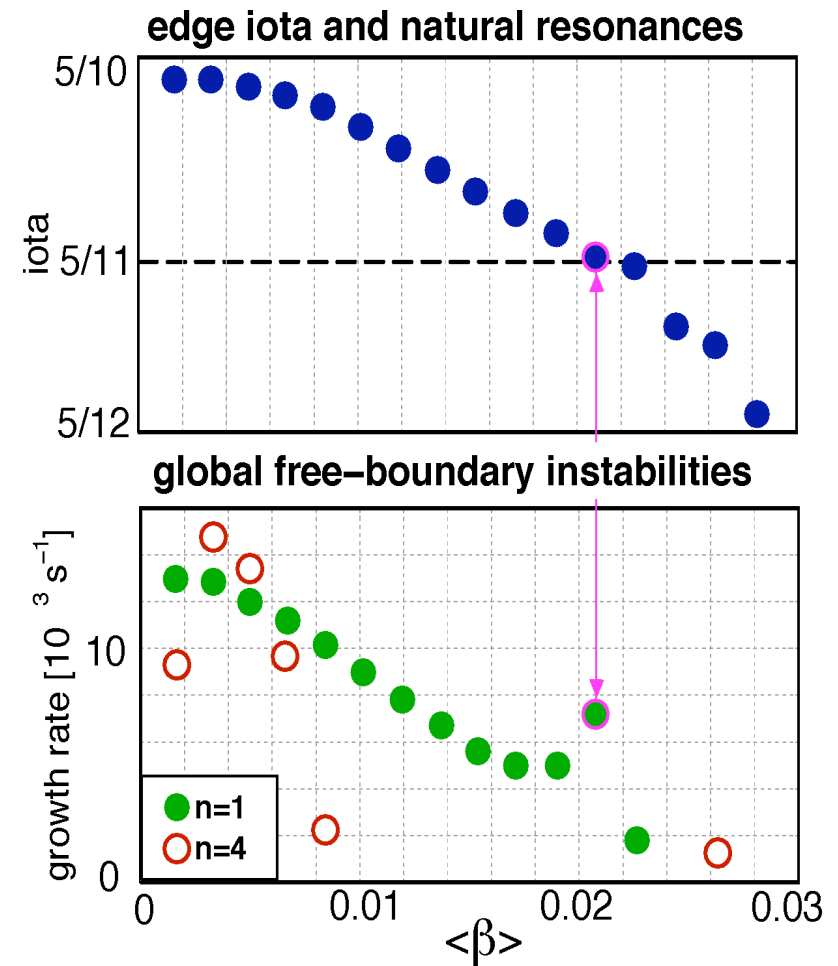
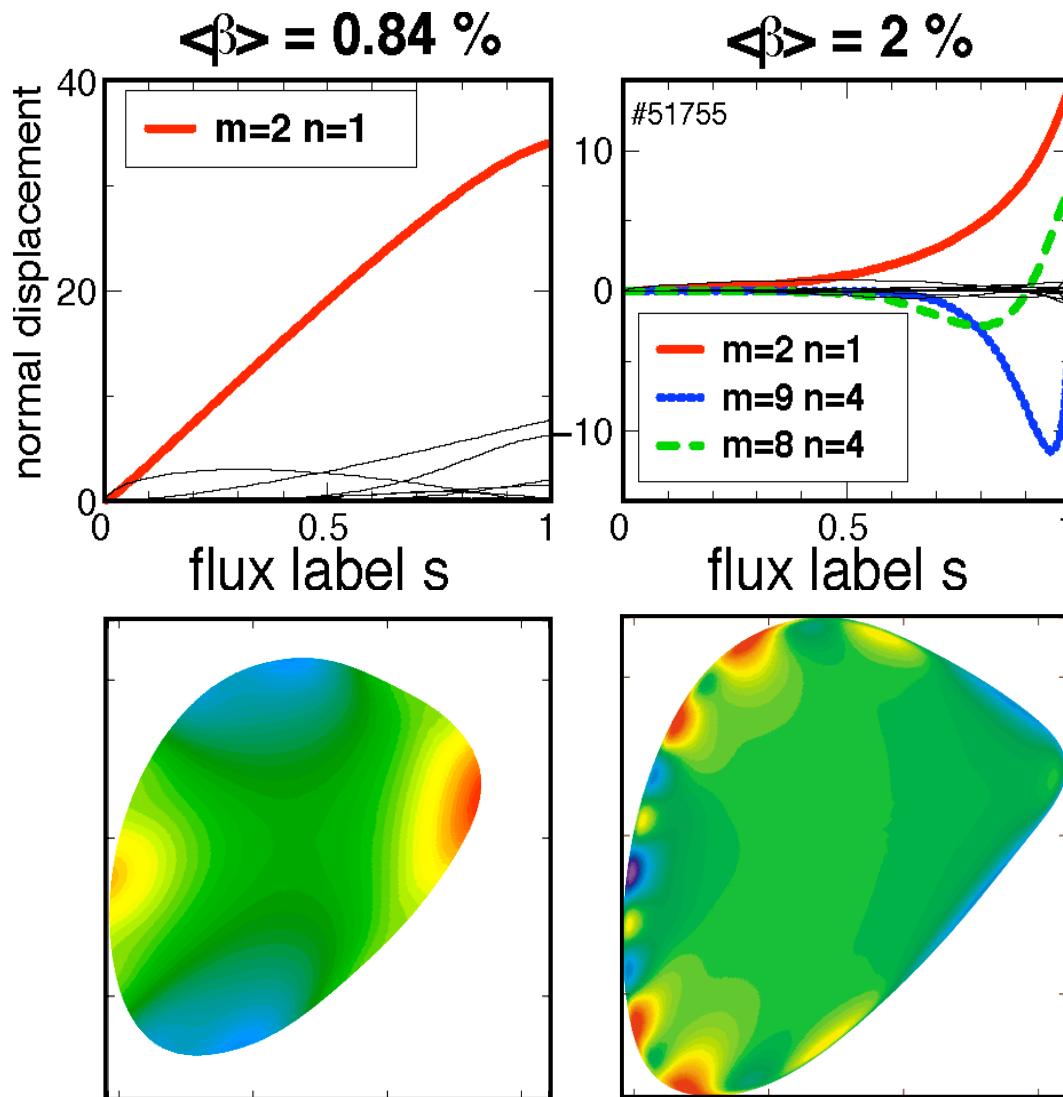
- Controlled iota scan, varying I_{TF} / I_M , fixed B , P_{NB}
- Flat-top phase
- Strong MHD clearly degrades confinement
- Strong MHD activity only in narrow ranges of external iota
- Equilibrium fitting indicates strong MHD occurs when edge iota \square 0.5 or 0.6 ($m/n=2/1$ or $5/3$)
- Strong MHD easily avoided by $\sim 4\%$ change in TF current

(M.C. Zarnstorff)

Linear Stability Calculations (CAS3D) Indicate 2/1 Should be Unstable in W7-AS

Mode Displacement & Perturbed Pressure

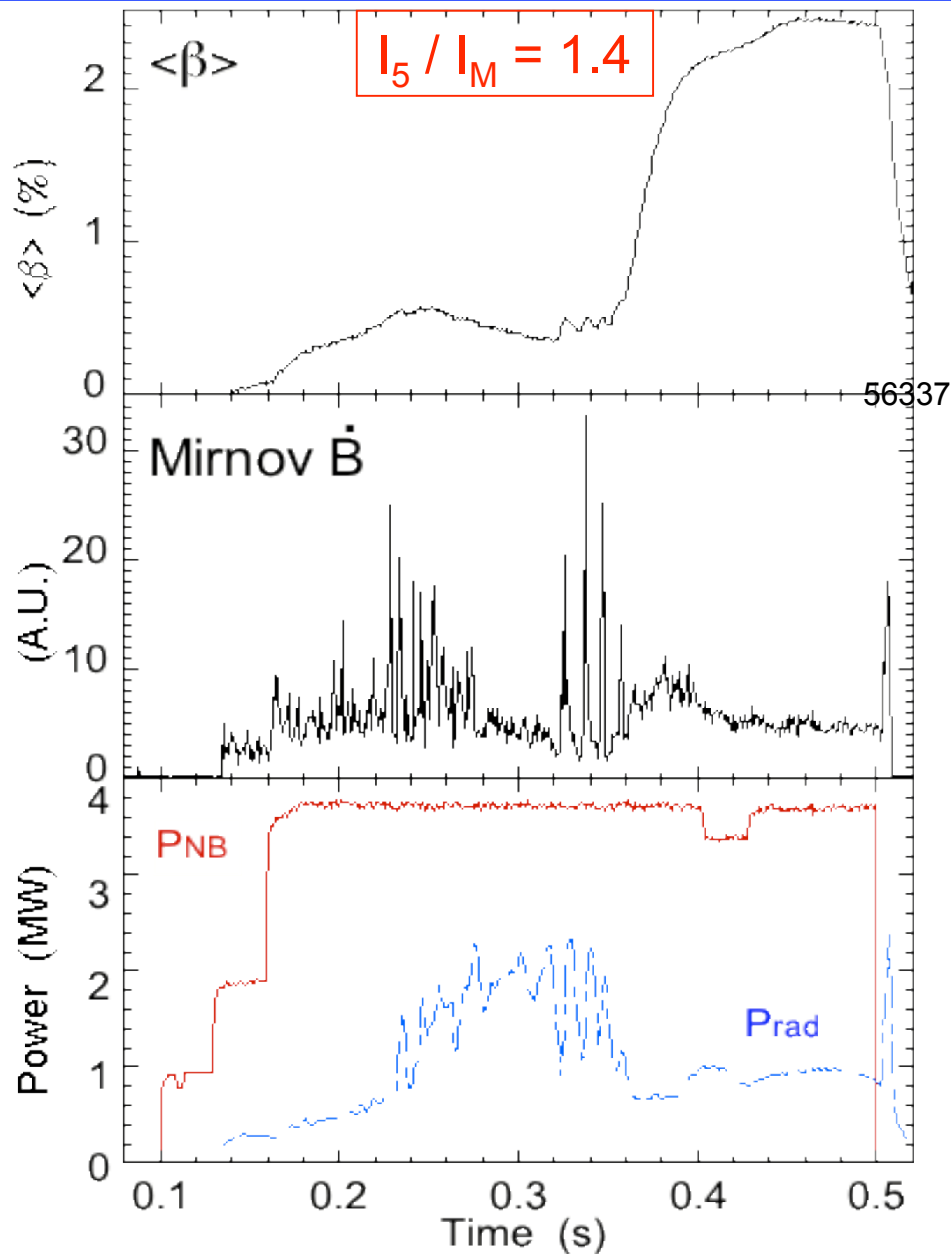
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**External global modes
most unstable at low β**

(C. Nuhrenberg)

High-n Instabilities Sometimes Observed in W7-AS



- Typical high- β plasmas are calculated to be ballooning stable. No high-n instabilities are observed.
- High-n instabilities are observed if T_e drops below ~ 200 eV. Probably a resistive instability.
- W7AS can vary the toroidal ripple or mirror ratio using 'corner coils' (I_5)
- For $I_5 > I_M$, very unstable low- β phase, then spontaneous transition and rise to moderate β .
- In later $\beta > 2\%$ phase, plasma calculated to be in ballooning 2nd stability regime.
How does it get there?

Experimental Studies of MHD Instabilities in LHD Also Show MHD Stability at Low β

- Beta dependence of MHD activity:
 - Core MHD activity suppressed with β
 - Edge MHD activity increased with β
- Optimization of R_{ax} : $R_{ax} > 3.5$ is better
- High A reduces Shafranov shift, can produce plasma with $\beta_{dia} \sim 4\%$
- Why are the MHD modes stabilized?
 - (a) Profile flattening caused by MHD mode?
 - (b) Stopping of mode rotation? (but frequency unchanged)
 - (c) Variation of magnetic surface due to β ?

(A. Ware/S. Sakakibara)

Plasma Boundary Has a Significant Influence on MHD Stability in Heliotrons

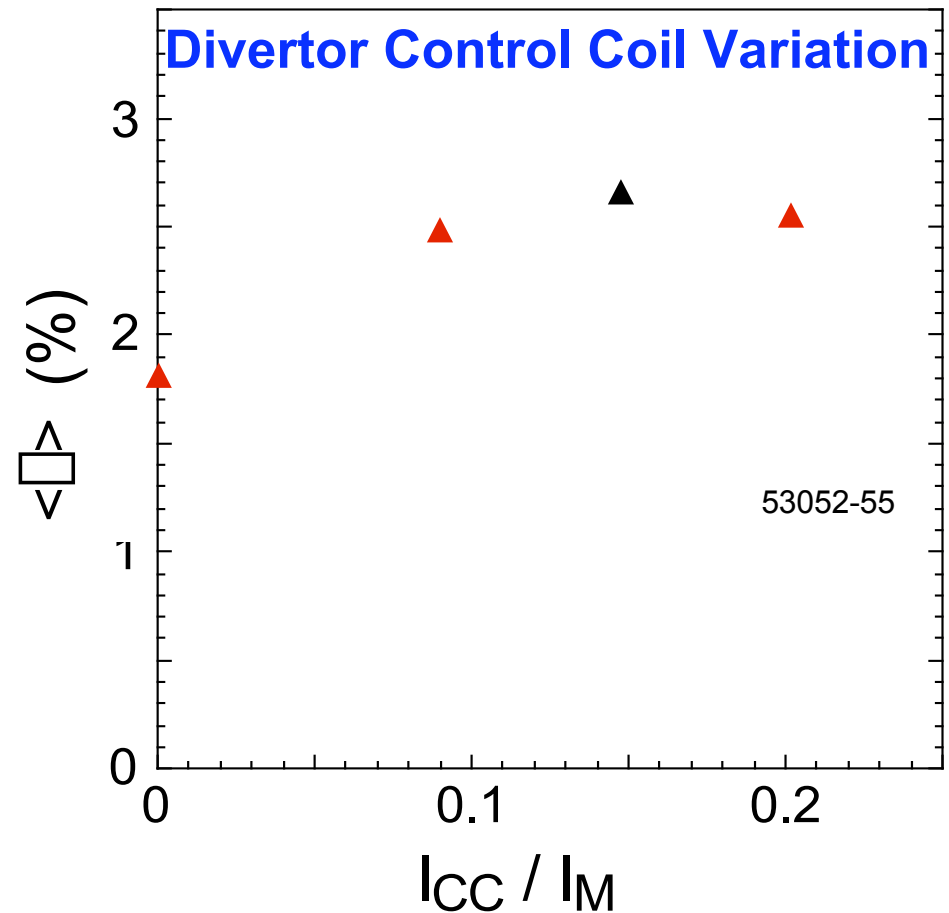
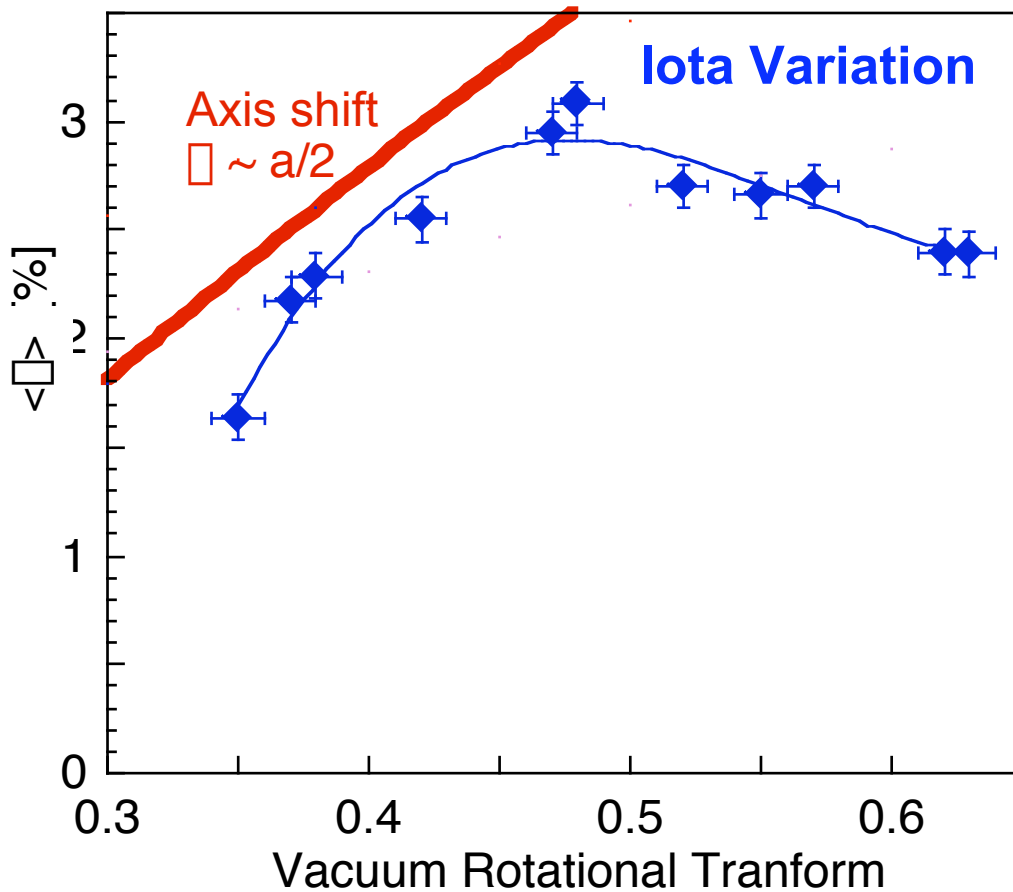
- Discrepancy on MHD equilibria & stability:
 - Experiment: $\langle \beta \rangle > 3\%$ plasmas
 - Theory: Strong MHD instabilities for fixed boundary plasmas
 - Finite pressure gradient observed beyond a clear vacuum LCFS
- Assume average flux surfaces in stochastic region
 - Inward shifted configurations have narrowest stochastic layer
 - For $\langle \beta \rangle = 3\%$, unstable for fixed boundary but marginally stable for free boundary
 - At high β , growth rates decrease with increasing $\langle \beta \rangle$ due to boundary modification
 - Density profile effects can be important in lowering growth rates as well



Is $\langle \Delta \rangle$ Limited by an Equilibrium Limit ?

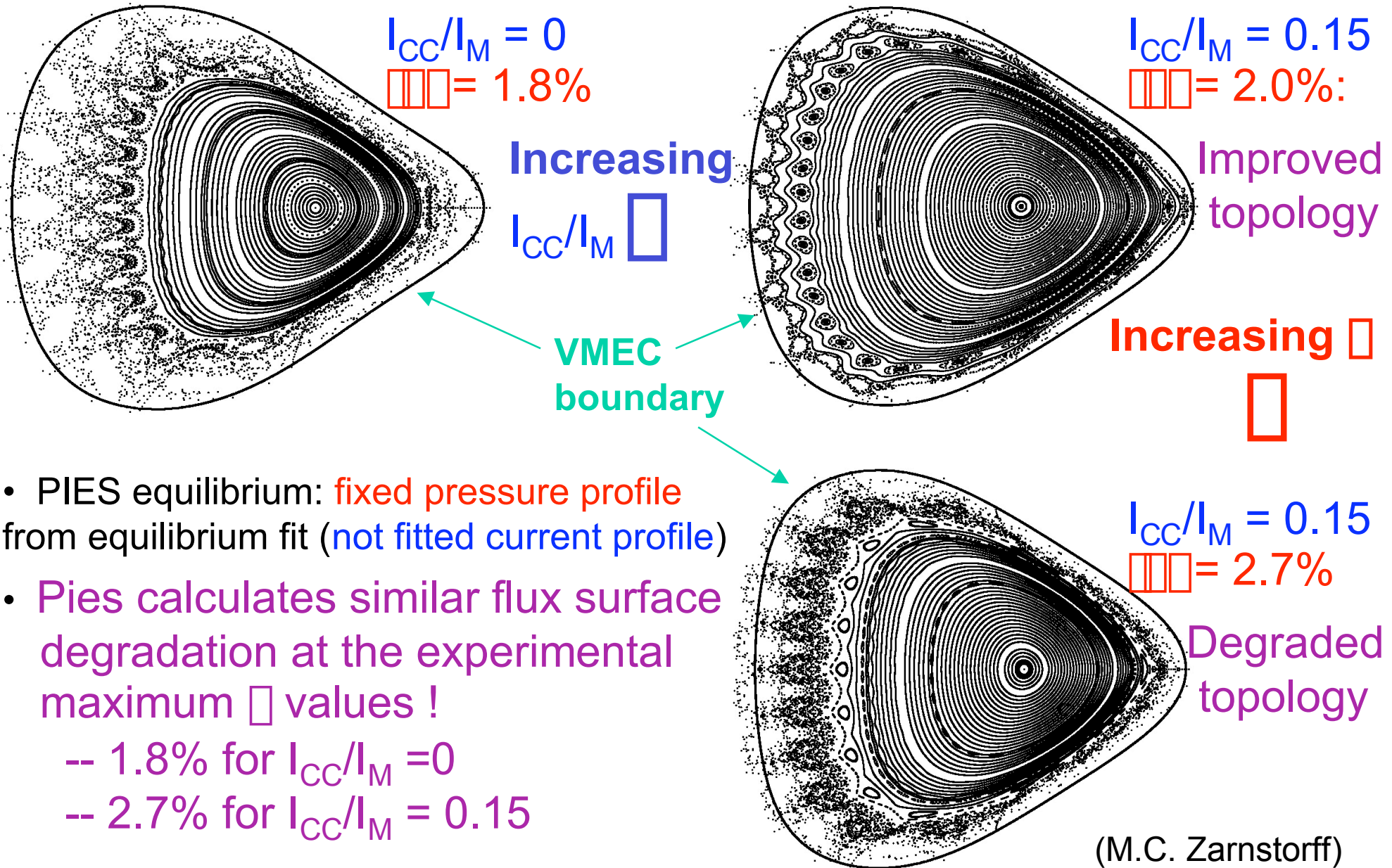
Maximum $\langle \Delta \rangle$ at low $\langle \Delta \rangle$ is close to classical equilibrium limit $\langle \Delta \rangle \sim a/2$

Control coil excitation does not affect iota or ripple transport



(M.C. Zarnstorff)

Control Coil Modulation Can Improved Flux Surface Topology as β is Increased

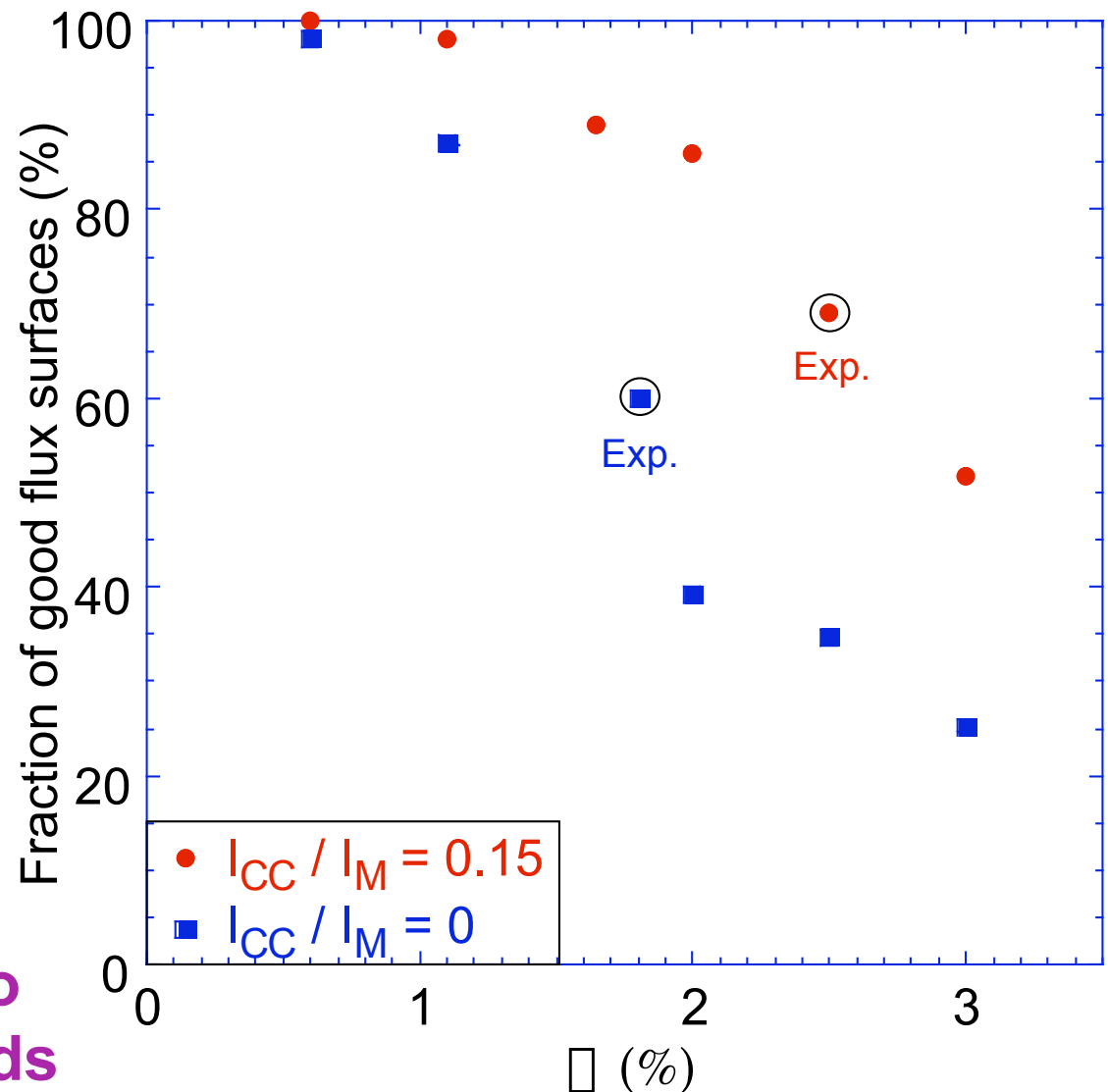


- PIES equilibrium: **fixed pressure profile** from equilibrium fit (**not fitted current profile**)
- Pies calculates similar flux surface degradation at the experimental maximum β values !
 - 1.8% for $I_{CC}/I_M = 0$
 - 2.7% for $I_{CC}/I_M = 0.15$

Degradation of Equilibrium May set W7-AS β Limit

- PIES equilibrium calculations indicate that fraction of good surfaces drops with β
- Drop occurs at higher β for higher I_{CC} / I_M

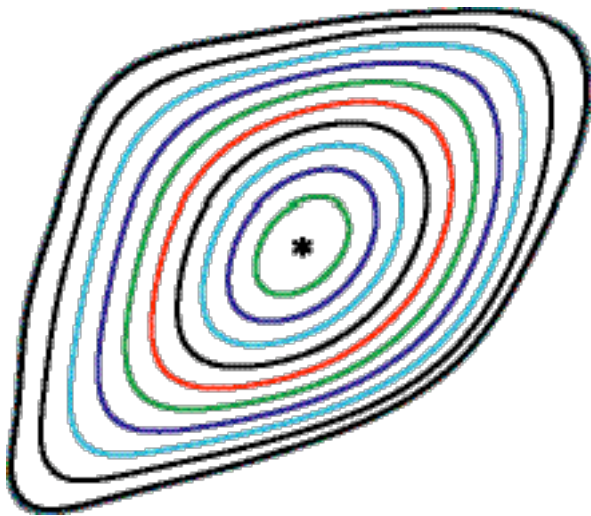
**Experimental β value
Correlates with loss of
~35% of minor radius to
stochastic fields or islands**



(M.C. Zarnstorff)

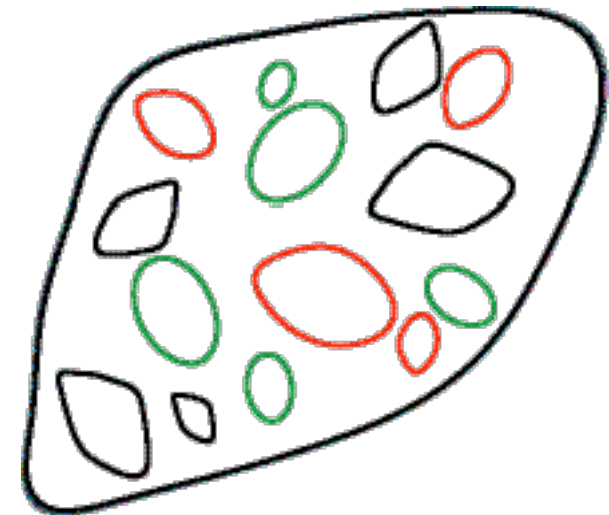
A New Proposed Model for Stellarator Equilibrium and Confinement \square Limit

- Is a stellarator equilibrium really like a simple container?



Add pressure up to point where container breaks
 \square Major leak: All energy lost

- Or is it more like a leaky sponge?



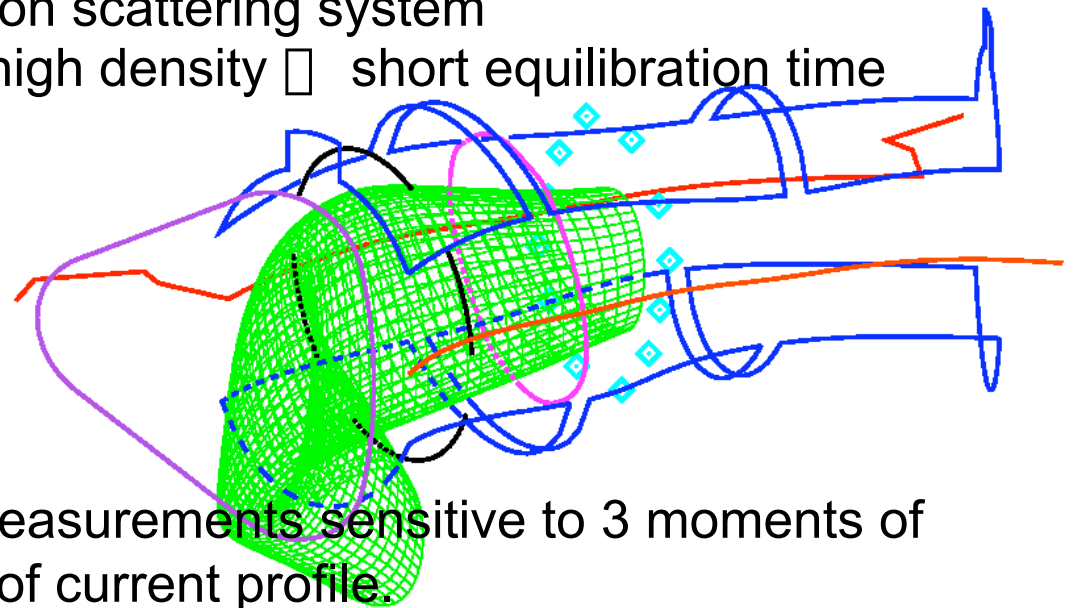
Add pressure to saturation point
 \square Holes expand as confinement degrades until pressure finally leaks as fast as it is absorbed

Recent Progress Made in Equilibrium Reconstructions

Need to reconstruct self-consistent equilibrium for further analysis:
pressure and iota profiles, plasma shape

- Available data:

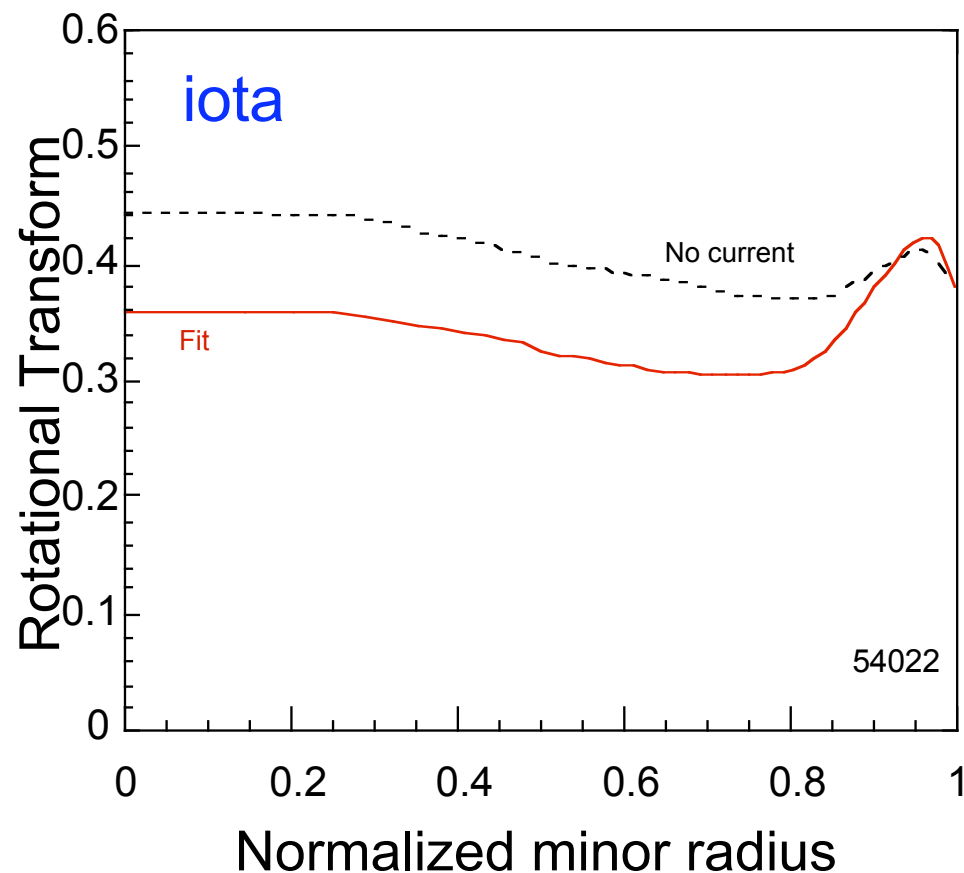
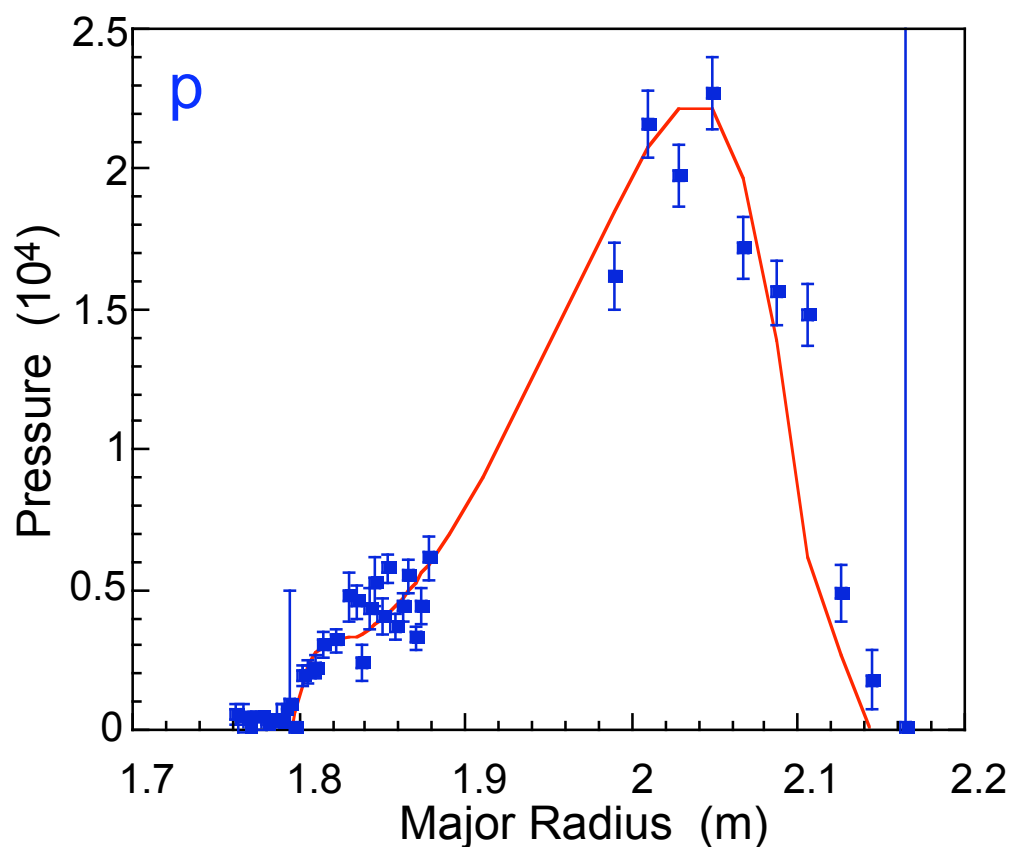
- 45 point single-time Thompson scattering system
assume $p_i = p_e$, due to very high density \square short equilibration time
- 19 magnetic measurements, including:
segmented Rogowski,
flux loops,
diamagnetic loops



- From SVD analysis: magnetic measurements sensitive to 3 moments of pressure profile and 2 moments of current profile.
- Adapted STELLOPT design-optimization code to be a free-boundary equilibrium reconstruction code

(M.C. Zarnstorff)

Reconstructed Self-Consistent W7-AS Equilibrium



- Reconstructed equilibrium of $\beta=3.4\%$ plasma
- Lower central iota, flatter profile
- Central $\beta=8.0\%$
- Edge pressure pedestal: present in many (but not all) high- β plasmas

(M.C. Zarnstorff)

Consistent Picture Emerging on Role of MHD Stability and the β Limit in Stellarators

- Both W7-AS and LHD show similar results regarding the ideal MHD stability limits:
 - Maximum β is not limited by MHD activity.
 - Maximum β reached is much higher than predicted linear stability thresholds
- Pressure driven MHD activity is observed in some cases at low or intermediate β
 - Usually saturates at harmless levels
 - Exists in narrow range of iota β easily avoided by adjusting coil currents
 - MHD at high β in LHD
- Predicted MHD stability correlates reasonably with observations at low β
 - Predicted MHD stability at high β depends sensitively on the boundary assumed

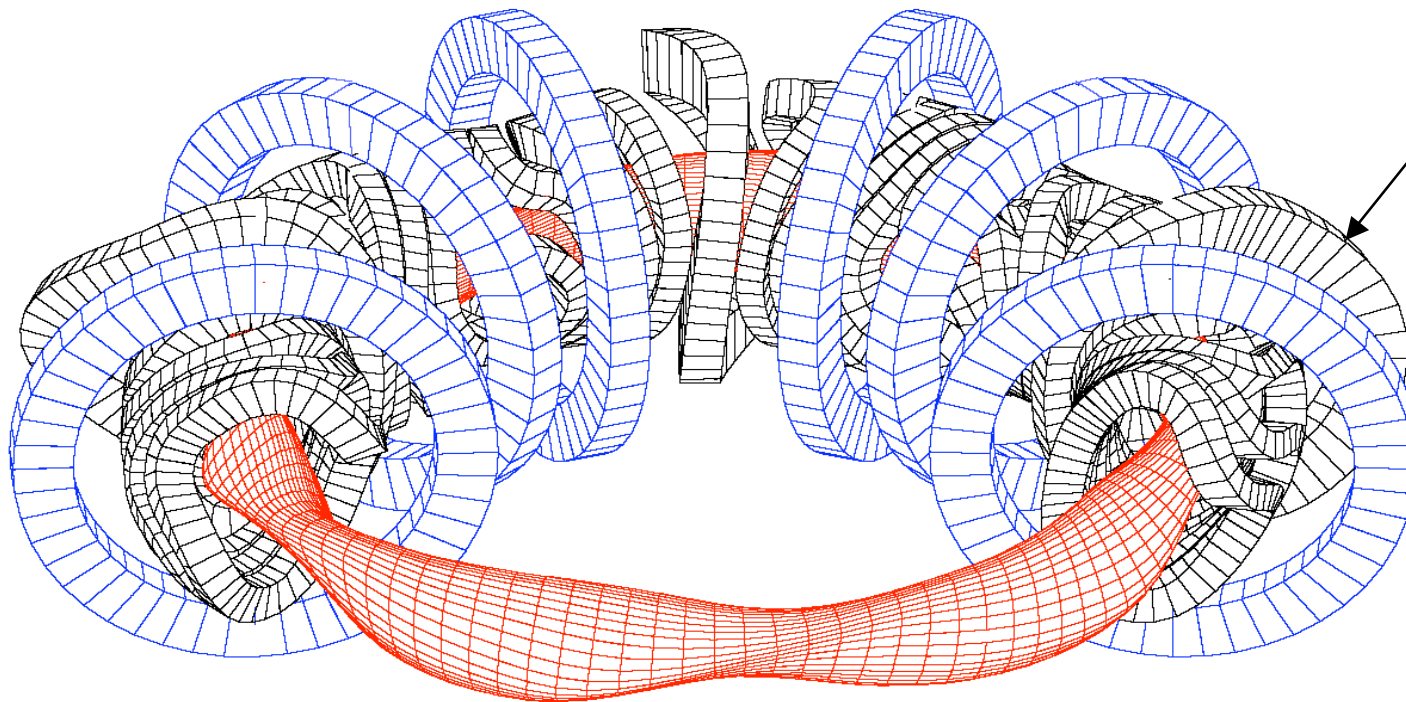
Maximum β Appears to be Controlled by Loss of Flux Surface Quality in Stellarators

- Maximum β correlated with calculated loss of $\sim 35\%$ of minor radius to stochastic magnetic field
 - May limit β
 - Leaky sponge model may be more appropriate
 - **Maximum β is not generally limited by MHD activity**
- Loss of minor radius has a significant effect on the predicted MHD stability properties
 - Generally stabilizing by removing edge resonances!
 - Ideal MHD stability predictions using fixed boundary VMEC equilibria are probably not valid at high β
 - Ideal MHD may still play a role in the limit at high β in some cases
 - Ideal MHD might be avoided at high β by small modulations of the boundary
 - BUT: Proximity to ideal MHD instability may contribute to deteriorating flux surfaces
- **More accurate equilibrium reconstructions with measured profiles and flux surfaces are clearly needed**
 - With sensitivity studies against possible variations in the discharge equilibria !

W7-AS – a flexible experiment

5 field periods, $R = 2$ m, minor radius $a \leq 0.16$ m, $B \leq 2.5$ T,
vacuum rotational transform $0.25 \leq \bar{\alpha}_{\text{ext}} \leq 0.6$

W7-AS



Flexible coilset:

- Modular coils produce helical field
- TF coils, to control rotational transform $\bar{\alpha}$
- Not shown:
 - divertor control coils
 - OH Transformer
 - Vertical field coils

Completed operation in 2002

(M.C. Zarnstorff)