

Progress on Systems Code and Revision of Previous Results

J. F. Lyon, ORNL

ARIES Meeting

Sept. 16, 2004



What's New Since June ARIES Meeting

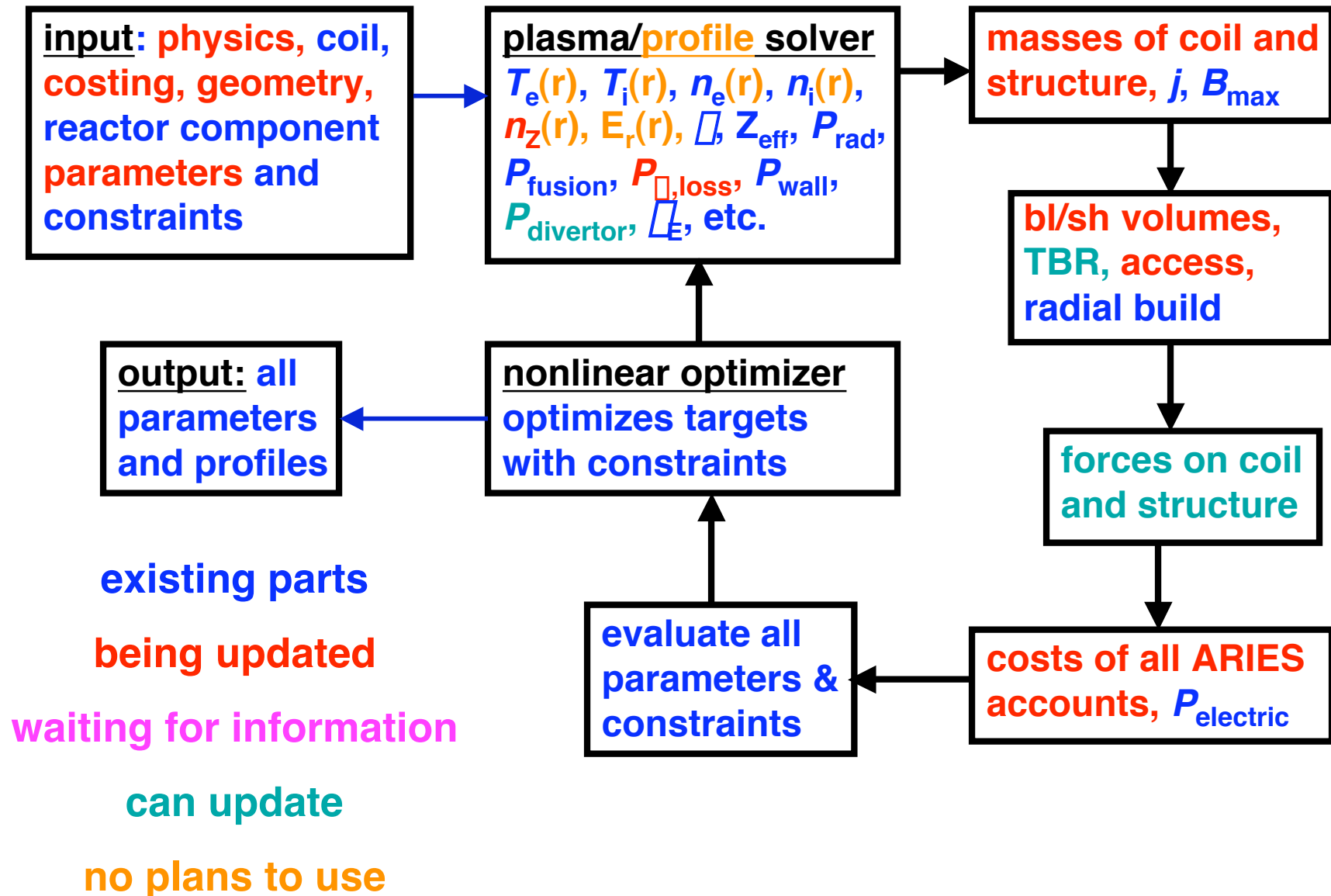
- **Progress on Systems/Optimization Code**
 - changes required and progress to date
 - issues and next steps
- **Revisions to 1-D POPCON calculations**
 - corrected He calculation
 - edge $T(r)$ and $n(r)$ pedestals; profile and sensitivity studies
- **Additional 0-D calculations**
 - examined two $A_\parallel$ cases for NCSX and extended scaling with $\langle p_{\text{wall}} \rangle$ for all cases
- **Comments on LHD reactor systems study**

Systems Code

- Purpose: integrate coil and plasma geometry, reactor constraints and costing
- Starting point -- last (mis)used in SPPS study
 - code written for tokamaks, revised for helical-coil stellarators (rotating ellipse, calculated $B_{\max}$ interpolating from database)
 - has ~ 7400 lines of code, highly interconnected
 - written ~15 years ago and last used ~10 years ago on computer platforms using math routines that no longer exist
- Changes needed even for *relative* comparisons
 - incorporate modular coil geometry (main components)
 - update physics & engineering (scaling, profiles, limits)
 - consistent treatment of impurities and edge
 - new models for blankets, shields, coils, structure
 - new costing for main components (waiting for numbers)
 - updated costing of other cost accounts (need consultation)
 - incorporation of maintenance periods

blue -- (partly) done, black -- in progress, red -- information needed

MHHOPT Reactor Optimization Code



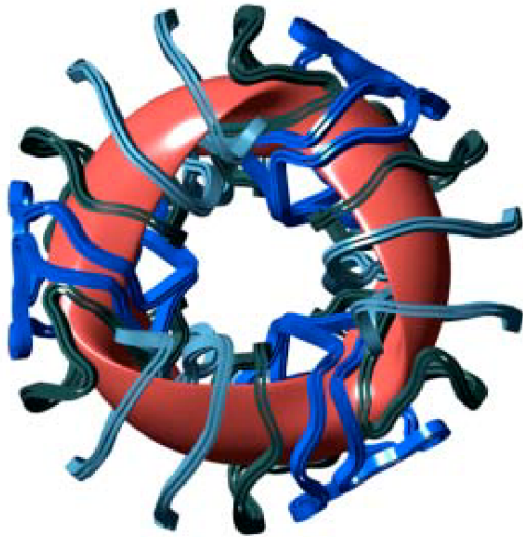
Systems Optimization Code

- Minimizes core cost or size or COE with constraints for a particular plasma and coil geometry using a nonlinear constrained optimizer
- Iterates on a number of optimization variables
 - plasma: $\langle T_i \rangle$, $\langle n_e \rangle$, H-ISS95; coils: width/depth of coils
 - reactor variables: B_0 , $\langle R \rangle$
- Large number of constraints allowed ($=$, $<$, or $>$)
 - P_{electric} , ignition margin, β limit, ISS-95 multiplier, radial build, coil j and B_{max} , plasma-coil distance, clearance between coils, blanket and shielding thicknesses, TBR, access for divertors and maintenance, etc.
- Large number of fixed parameters for plasma and coil configuration, plasma profiles, transport coefficients, **cost component algorithms**, and engineering model parameters
- Calculates a large number of parameters
 - plasma: β , Z_{eff} , power components (**radiation**, $\beta \Rightarrow i$, $\beta \Rightarrow e$), β losses, etc.
 - coils: components volumes and **costs**, j , B_{max} , **forces**
 - reactor variables: blanket volumes, TBR, neutron wall loading, **divertor area**, access between coils, radial build, etc.
 - costs: **equipment cost**, **annual operating cost**, **total project cost**, **CoE**

Input Parameters

- **Configuration geometry**
 - plasma aspect ratio, surface area, coil aspect ratio, closest approach aspect ratio, Δ_{limit} , $\Delta(r)$, ~~ripple~~_{effective}(r), etc.
- **Reactor component parameters**
 - inside & outside shield thickness; coil width and depth
 - blanket thickness inside & outside, under and **between** coils
 - coil case & vacuum vessel thickness, dimensions of modular coils and VF coils; scrapeoff thickness
 - first wall and reflector thickness; coil to vacuum vessel gap
 - ~~allowable nuclear heating in coil~~; $j_{\text{max}}(B)$
 - blanket energy multiplication
- **Cost assumptions**
 - modular and **VF** costs /kg
 - **costs** and multipliers for blanket and shield
 - **duty factor**, inflation, **safety assurance**

Four Configurations Now Studied

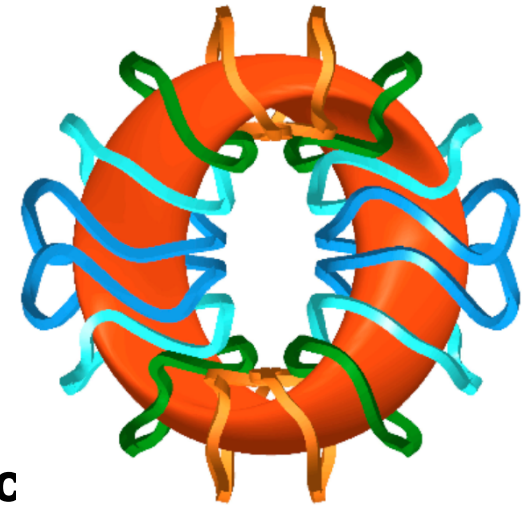


NCSX

port or
sector
(end)
access

MHH2

access
through
ports



both quasi-axisymmetric

Key Configuration Properties	NCSX-1	NCSX-2	MHH2-8	MHH2-16
Plasma aspect ratio $A_p = \langle R \rangle / \langle a \rangle$	4.50	4.50	2.70	3.75
Wall (plasma) surface area / $\langle R \rangle^2$	11.80	11.95	19.01	13.37
Min. plasma-coil separation ratio $\langle R \rangle / \square_{\min}$	5.90	6.88	4.91	5.52
Min. coil-coil separation ratio $\langle R \rangle / (c-c)_{\min}$	10.07	9.38	7.63	13.27
Total coil length / $\langle R \rangle$	89.7	88.3	44.1	64.6
$B_{\max, \text{coil}} / \langle B_{\text{axis}} \rangle$ for 0.4-m x 0.4-m coil pack	2.10	1.84	3.88	2.77

- $\langle R_{\text{coil}} \rangle / \langle R \rangle$ constant for each case, can't change separately

Output

- **Plasma parameters and profiles**
 - $\langle R \rangle$, $\langle B_{\text{axis}} \rangle$, W_{plasma} , $\langle \beta \rangle$, β^* , n_{Fe}/n_e , n_{O}/n_e , Z_{eff}
 - $\langle T \rangle$, T_{i0} , $T_{i,\text{edge}}$, T_{e0} , $T_{e,\text{edge}}$, β_0/T_{e0} , $\langle n \rangle$, n_{i0} , n_{e0} , $\langle n \rangle/n_{\text{Sudo}}$, n_{DT}/n_e ,
 - ignition margin, P_{fusion} , P_{electric} , P_{neutron} , P_{charged} , P_{divertor} , components of P_{rad} and P_{wall} , P_{loss}
- **Coil parameters**
 - modular & VF coil dimensions, currents, forces, inductance, stored energy, j , B_{max} , case thickness
- **Reactor parameters**
 - blanket area accessible and blocked, inboard and outboard shield thickness, cryostat gap, access between coils

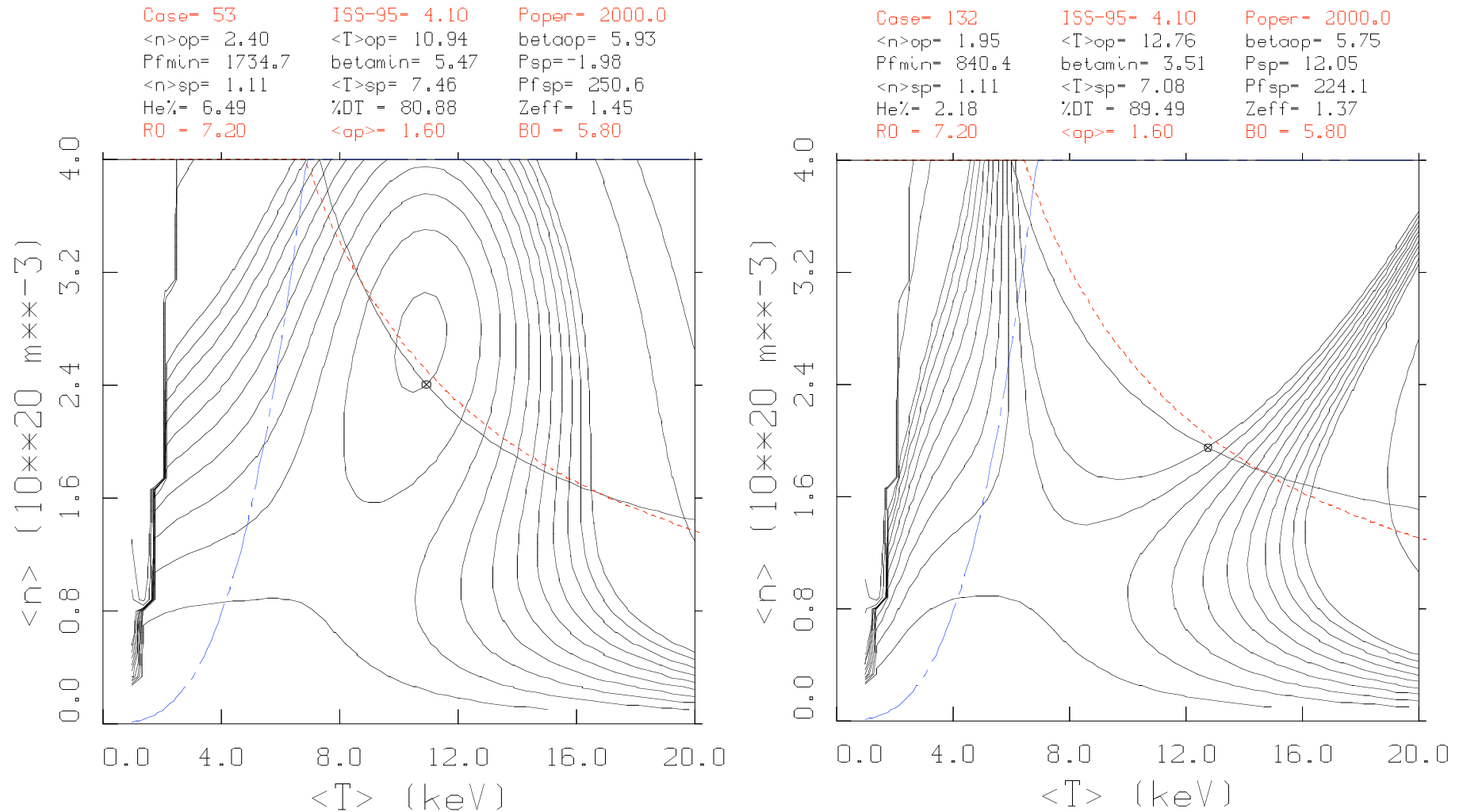
Output (cont.)

- **Cost elements**
 - land & structures; power supplies; impurity control; heat transport; power conversion; startup power
 - blankets & first wall; shields; modular & VF coils; structure; vacuum vessel
 - turbine plant equipment; electric plant equipment; misc. plant equipment; special materials; **total direct cost**
 - construction; home office; field office; owner's costs; project contingency; construction interest; construction escalation; **total capital cost**
 - unit direct cost; unit base cost; total unit cost; capital return; O&M costs; blanket/first wall replacement; decommissioning allowance; fuel costs; **cost of electricity**
- **Summary of all component masses & mass utilization**
- **Dimensions of each element in the radial build**

Revision to 1-D (POPCON) Calculations

- **Purpose of 1-D calculations:**
 - test different profiles, physics models and assumptions for incorporation into systems code
 - examine effect of assumptions on operating point
- **Corrected error in calculation of helium concentration**
 - this affected n_{DT}/n_e , P_{fusion} , etc.
 - removes earlier concern on $\bar{\alpha}_{He}/\bar{\alpha}_E < 2$ being too low (now > 6)
- **Added edge pedestals to simulate edge cooling from enhanced (neoclassical impurity) edge radiation**
 - small effect, but more consistent with large edge radiation
- **Will later update confinement scaling ISS-95 --> ISS-04**
 - small effect, but dimensionally correct and fits data better
 - basis for assumed H-ISS values

Effect of Correction to n_{He} Calculation

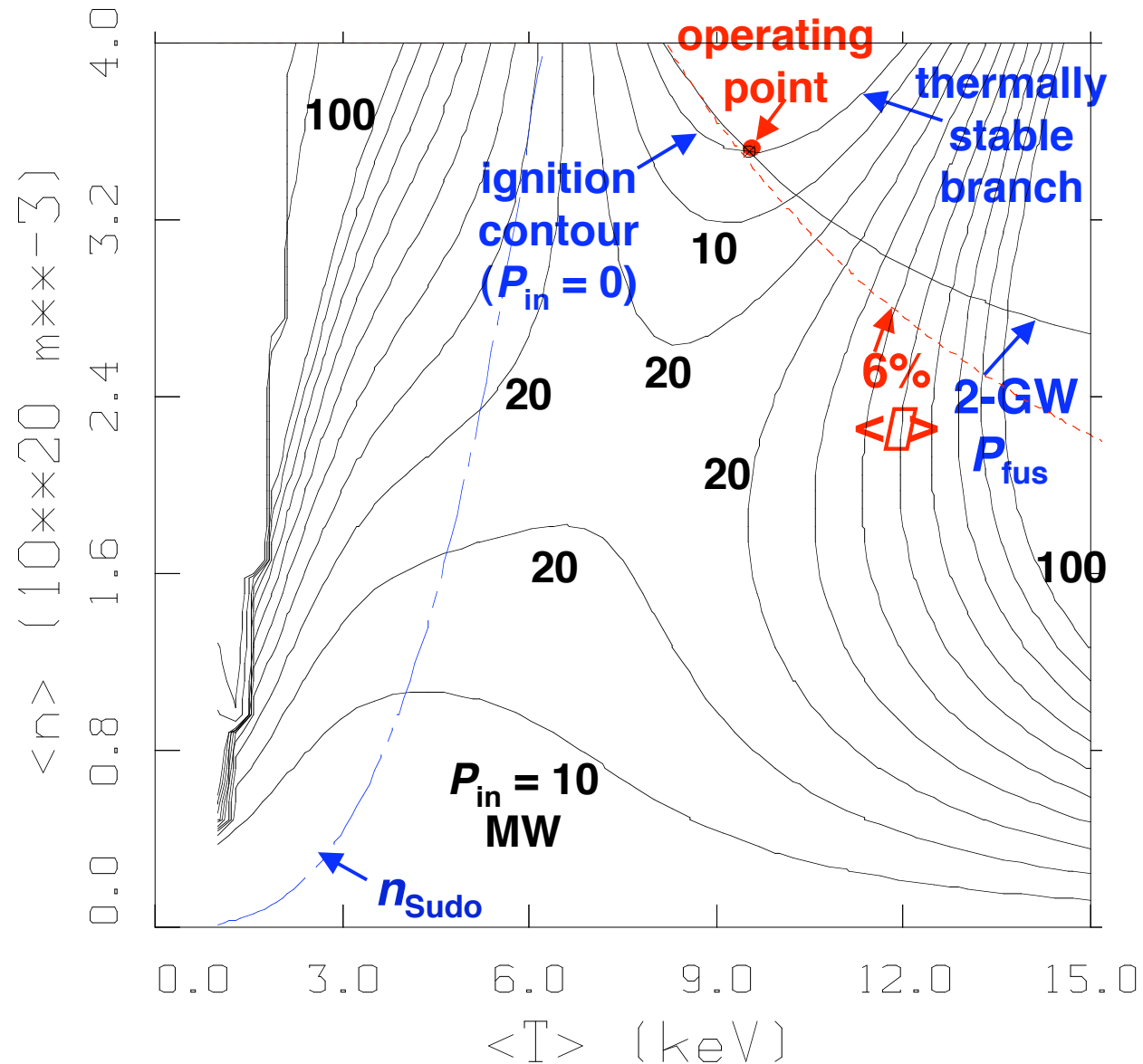


- Previously required $\beta_{\text{He}}^*/\beta_E < 2$, now > 6 OK
- Minimum H-ISS95 $\Rightarrow 3.7$ for a stable operating point

NCSX-1: $\beta_E/\beta_E^{\text{ISS-95}} = 4.2$, $\langle T \rangle = 9.5$ keV, $\langle n \rangle = 3.5 \cdot 10^{20} \text{ m}^{-3}$, $\langle \beta \rangle = 6.1\%$

H-ISS95 =

$\beta_E/\beta_E^{\text{ISS-95}}$



- $\beta_E^{\text{ISS-95}} = 0.26 P_{\text{heating}}^{-0.59} \langle n_e \rangle^{0.51} \langle B_{\text{axis}} \rangle^{0.83} \langle R \rangle^{0.65} \langle a \rangle^{2.21} \langle \beta \rangle^{0.4}$

Plasma Parameters from 1-D Power Balance

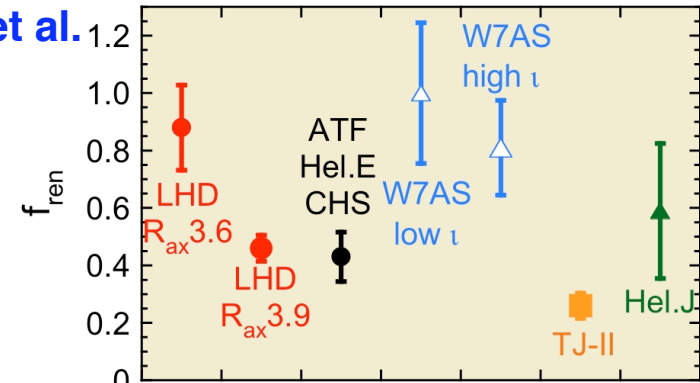
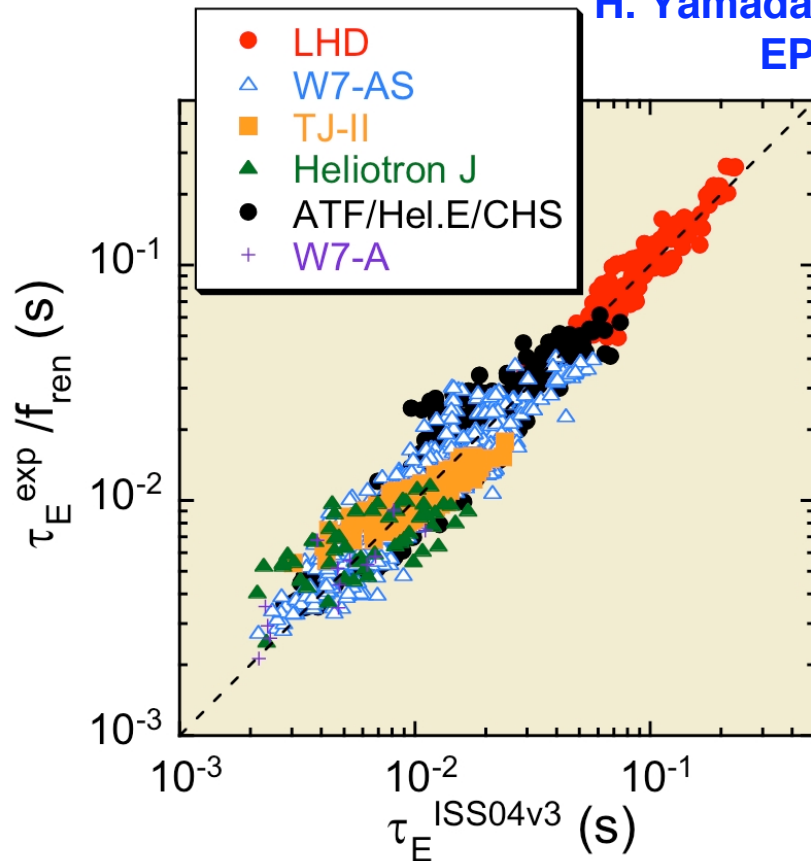
	NCSX-1	NCSX-2	MHH2-8	MHH2-16
$\langle R \rangle$ (m)	6.22	6.93	6.19	6.93
$\langle a \rangle$ (m)	1.38	1.54	2.29	1.85
$\langle B_{\text{axis}} \rangle$ (T)	6.48	5.98	5.04	5.46
H-ISS95	4.15	4.20	3.75	4.10
$\langle n \rangle (10^{20} \text{ m}^{-3})$	3.51	2.89	2.05	2.43
f_{DT}	0.841	0.837	0.837	0.839
f_{He}	0.049	0.051	0.051	0.050
$\langle T \rangle$ (keV)	9.52	9.89	9.92	9.74
$\langle \beta \rangle$ (%)	6.09	6.12	6.13	6.09

- ISS-95 of 3.75 to 4.2 is required; present stellarator experiments have up to 2.5
- ISS-2004 scaling indicates $\langle n_{\text{eff}} \rangle^{-0.4}$ improvement, so compact stellarators should have high H-ISS values

ISS-95 Confinement Scaling Is Being Updated

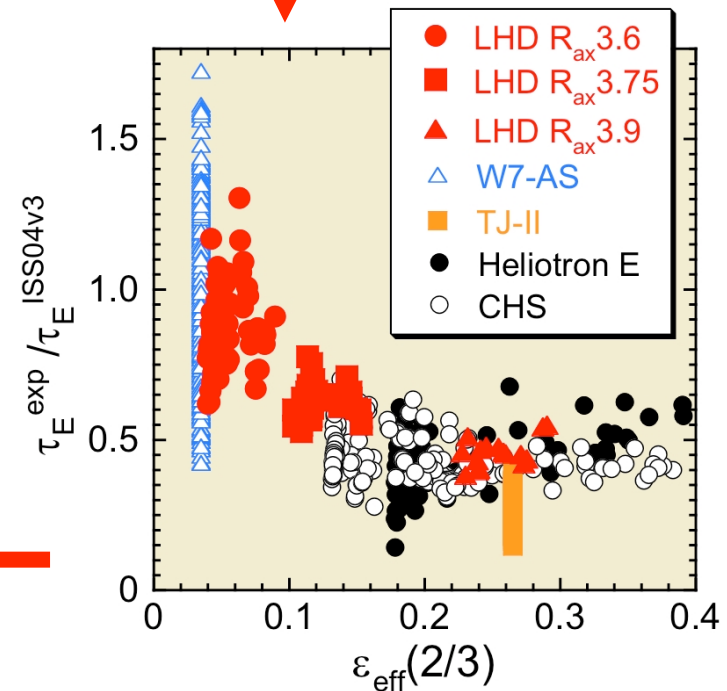
$$\tau_E^{ISS04v3} = 0.148 a^{2.33} R^{0.64} P^{0.61} \bar{n}_e^{0.55} B^{0.85} \left[\frac{a}{R} \right]^{0.41} \left[\frac{a}{R} \right]_{Bohm}^* \left[\frac{a}{R} \right]^{0.90} \left[\frac{a}{R} \right]^{0.14} \left[\frac{a}{R} \right]_b^{*0.01}$$

H. Yamada, J. Harris et al.
EPS 2004



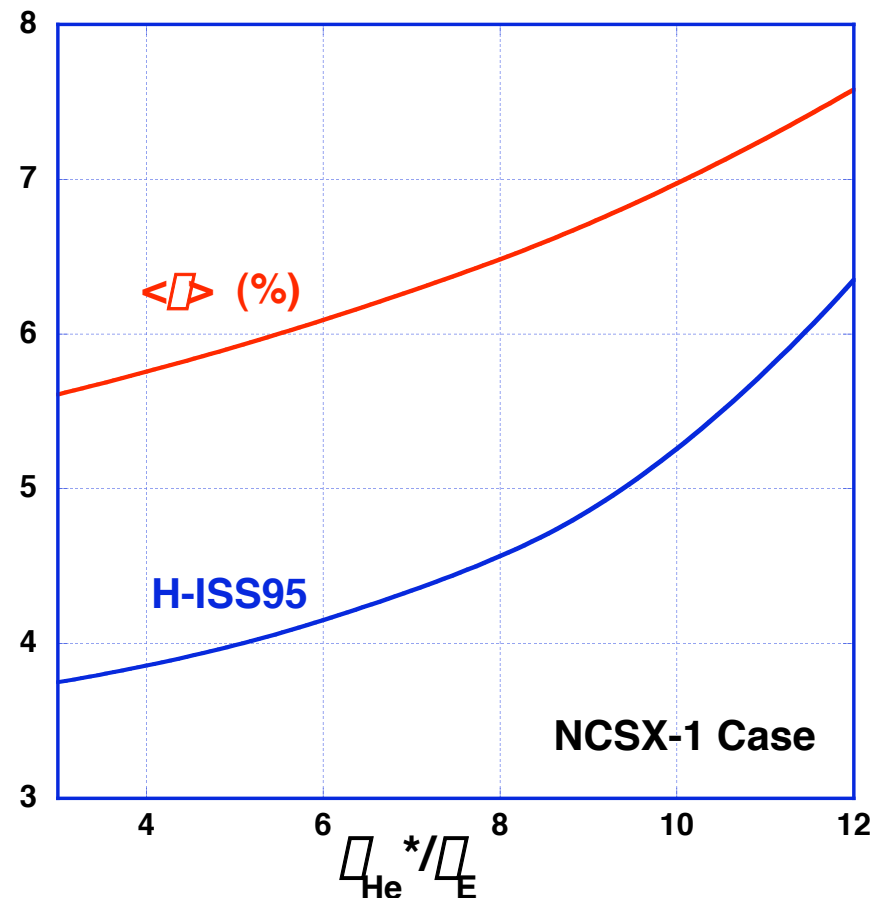
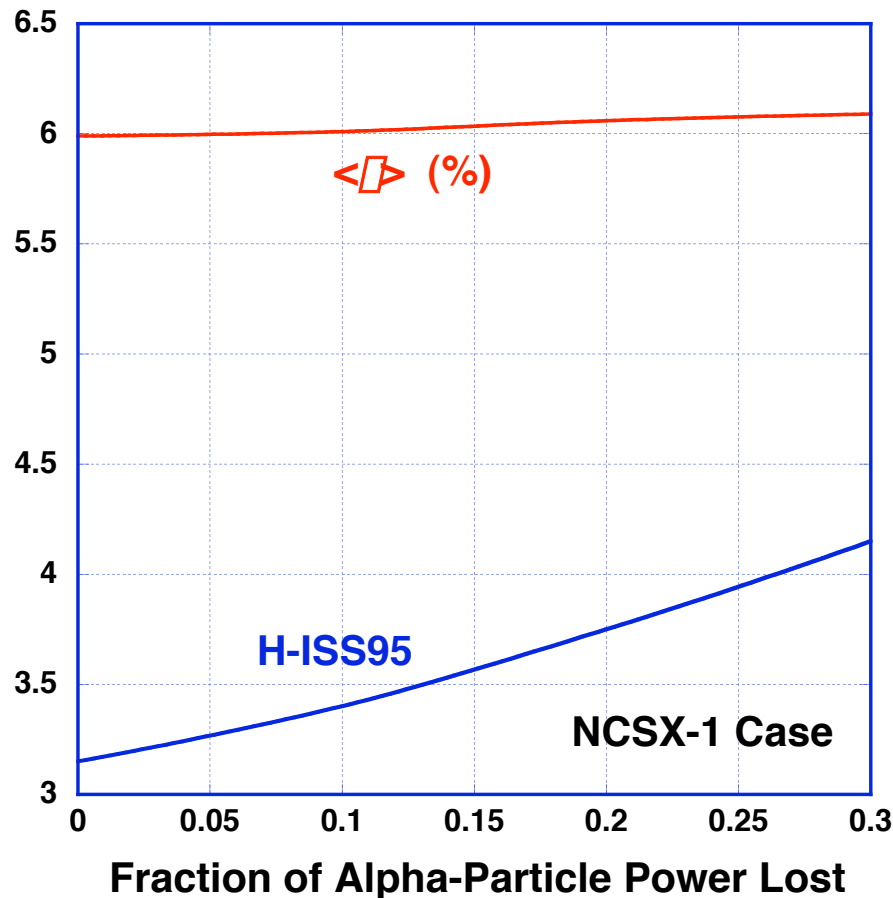
Experiments

$\sim \epsilon_{eff}^{-0.4}?$



- $\tau_E \sim \epsilon_{eff}^{-0.4}$ should give large H-ISS for low ϵ_{eff} NCSX configuration
- Lays basis for higher H-ISS values

H-ISS95 Is Sensitive to Some Assumptions



- Need to control alpha-particle power loss and helium recycling back into plasma -- both *divertor* issues

Parameters Insensitive to Profile Assumptions

Variation	$\bar{n} 10^{20} \text{ m}^{-3}$	$\bar{T}$ keV	H-ISS95	$\bar{W}$ %
Base case	3.51	9.52	4.15	6.09
Peaked n	3.36	9.85	4.00	6.03
0.1 n_{pedestal}	3.53	9.46	4.10	6.09
0.2 n_{pedestal}	3.57	9.34	4.05	6.09
T parabolic	3.23	10.82	4.40	6.36
T parabolic ²	3.60	9.01	4.00	5.92
0.1 T_{pedestal}	3.28	10.68	4.40	6.37
0.2 T_{pedestal}	3.22	11.11	4.50	6.50
Peaked n_z	3.42	9.97	4.15	6.21
T screening	3.48	9.15	3.75	5.81

0-D (Volume-Average) Calculations

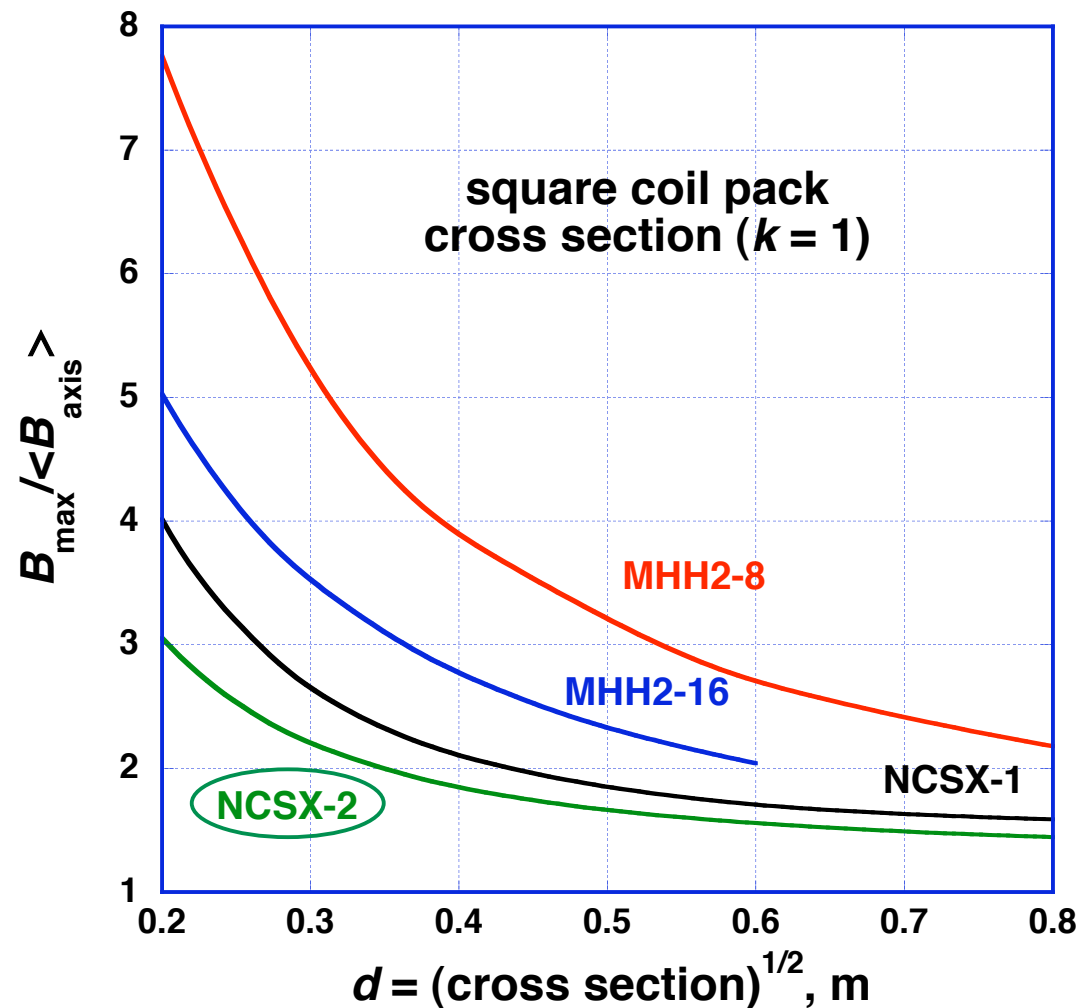
PURPOSE

- **Allows analytic treatment of**
 - connection between different device parameters
 - effect of different assumptions and constraints
- **Validates modules needed for systems code**

ADDITIONS

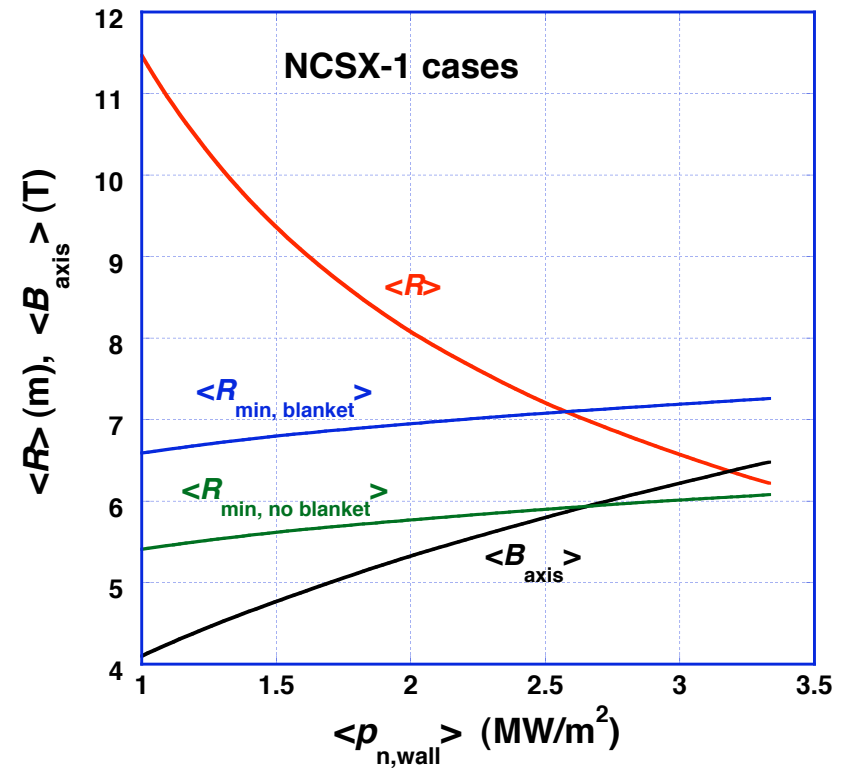
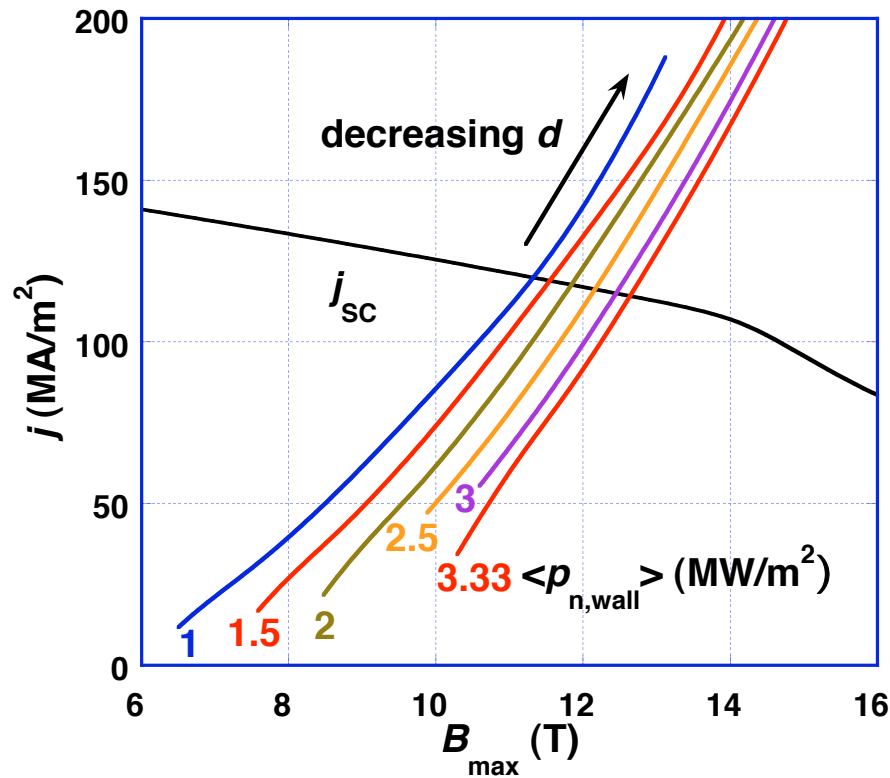
- **NCSX case with different $A_{\square}$ (2/25/03 case)**
- **Superconducting coil constraint**
- **Varied p_{wall} from 1 to 3.3 MW/m² (assumed peak 1.5 times higher) to study variation in global parameters**

Added 2/25/03 (NCSX-2) Case



- Smaller plasma-coil spacing leads to less convoluted coils and lower $B_{\max}/\langle B_{\text{axis}} \rangle$
- Minimum coil-coil separation distance determined $k_{\max}$

NCSX-1 Values Limited to $p_{n,\max} = 5 \text{ MW/m}^2$



- $\langle R \rangle = 6.22 \text{ m}$, $\langle B_{\text{axis}} \rangle = 6.48 \text{ T}$, $B_{\max} = 12.65 \text{ T}$
- j_{coil} approximately constant
- $\langle R \rangle$, $\langle B_{\text{axis}} \rangle$, $B_{\max}$ & d are constrained for other cases by radial build to lower $\langle p_{n,\text{wall}} \rangle$ (2.13–2.67 MW/m²)

Scaling Relations for Reactor Parameters

- **Fusion power** red indicates configuration-specific parameters
 - $P_{\text{fusion}} \sim \langle \beta \rangle^2 \langle B_{\text{axis}} \rangle^4 \langle R \rangle^3 / A_p$
 - $p_{n,\text{wall}} / 1.5 = \langle p_{\text{wall}} \rangle = 0.8 P_{\text{fusion}} / [\langle R \rangle^2 (A_{\text{wall}} / \langle R \rangle^2)]$
- **Coil-geometry related** $sh = sh_2 + c \times \ln(\langle p_{\text{wall}} \rangle)$
 - $\langle R \rangle = A_{\square} (\text{so} + \text{fw} + \text{bl} + \text{sh} + \text{vv} + \text{gaps} + 0.5 dk^{1/2})$ *constraint*
 - $j_{\text{coil}} = I_{\text{coil}} / d^2 = \langle B_{\text{axis}} \rangle \times R [I_{\text{coil}} / \langle B_{\text{axis}} \rangle \times R] / d^2$
 - $j_{\text{SC}}(B_{\text{max}})$ and d, k from $B_{\text{max}} / \langle B_{\text{axis}} \rangle$
- **Cost-related (rationale for $\langle p_{\text{wall}} \rangle$ emphasis**
 - blanket, shield, vacuum vessel, coil structure $\sim$ wall area $\sim P_{\text{fusion}} / \langle p_{n,\text{wall}} \rangle$, but $\langle p_{n,\text{wall}} \rangle$ configuration constrained
 - fw/blanket replacement $\sim$ frequency $\times$ cost
 $\sim 1 / \langle p_{n,\text{wall}} \rangle \times P_{\text{fusion}} / \langle p_{n,\text{wall}} \rangle \sim P_{\text{fusion}}$ independent of $\langle p_{n,\text{wall}} \rangle$
but actual cost depends on specifics
 - volume of coils $\sim L_{\text{coil}} I_{\text{coil}} / j_{\text{coil}} \sim C \times P_{\text{fusion}}^{7/8} / (\langle p_{n,\text{wall}} \rangle^{5/8} \langle \beta \rangle^{1/2} j_{\text{coil}})$
 $C = (L_{\text{coil}} / \langle R \rangle) (I_{\text{coil}} / \langle B_{\text{axis}} \rangle \times R) A_p^{1/2} / (A_{\text{wall}} / \langle R \rangle^2)^{5/8}$, C / j_{coil} constant

Main Reactor Parameters from 0-D Study

	NCSX-1	NCSX-2	MHH2-8	MHH2-16
$\langle p_{n,wall} \rangle$ (MW/m ²)	3.33	2.67	2.13	2.4
$\langle R \rangle$ (m)	6.22	6.93	6.19	6.93
$\langle a \rangle$ (m)	1.38	1.54	2.29	1.85
$\langle B_{axis} \rangle$ (T)	6.48	5.98	5.04	5.46
B_{max} (T)	12.65	10.9	14.9	15.2
j_{coil} (MA/m ²)	114	119	93	93
k_{max}	3.30	5.0	2.78	1.87
coil width (m)	0.598	0.719	0.791	0.502
coil depth (m)	0.181	0.144	0.286	0.268
radial gap (m)	0.026	0.012	0.007	0.005
Coil volume (m ³)	60.3	63.4	61.4	60.3
Wall area (m ²)	480	600	750	667

- Wall (blanket, shield, structure, vacuum vessel) area smallest for NCSX-1
- chose NCSX-1 (8/1/03 case) for more detailed study

LHD Reactor Study (T. Dolan)

- Based on LHD plasma and coil configuration
- Uses port maintainence scheme and three blanket + cooling models (RAFS + Flibe, Va + Li, SiC + PBLi)
- Based on Miller's costing code with some new values
- H-ISS95 limited to 2, $\langle \beta \rangle$ to 4%, $B_{\max} = 13$ T
 - consistent with LHD performance, higher β_{eff} value
- Base case has $R = 14.4$ m, $B_{\text{axis}} \sim 5.5$ T, H-ISS95 = 1.7, $\langle \beta \rangle = 3\%$, $P_{\text{fusion}} = 4.5$ GW ($P_{\text{electric}} = 1.94$ GW), $\langle p_{\text{wall}} \rangle = 2.1$ MW/m², $j_{\text{coil}} = 30$ MA/m², $k = 2$, $f_{\text{loss}} = 0.1$, $\beta = 40\%$
- Studied CoE variation with T_0 , n & T profiles, $\langle \beta \rangle$, k , plasma-wall dist, shield-coil gap, $B_{\max}$, $\langle p_{\text{wall}} \rangle$, P_{electric}

Summary

- **Progress on Systems/Optimization Code**
 - added modular coil geometry and updated physics models
 - treatment of impurities and edge and new models for blankets, shields, coils, structure in progress
 - information needed on new costing for main components and updated costing of other cost accounts
- **Revised 1-D POPCON calculations**
 - corrected He calculation
 - insensitive to profiles, edge $n(r)$ & $T(r)$ pedestals
 - more sensitive to alpha-particle losses and helium $\bar{\rho}_p^*$
- **0-D -- added 2/25 NCSX case, superconducting coil constraint, and extended scaling with $\langle p_{\text{wall}} \rangle$**
- **Examined LHD reactor systems study**